# Searching for High Energy Neutrinos with the AMANDA-II DETECTOR 

by

Jodi Ann Cooley-Sekula

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# Searching for High Energy Neutrinos with the AMANDA-II Detector 

Jodi Ann Cooley-Sekula<br>Under the supervision of Professor Albrecht Karle At the University of Wisconsin - Madison

The Antarctic Muon and Neutrino Detector Array (AMANDA) is designed to detect high energy neutrinos from extragalactic sources. It uses the south polar ice cap as both a target and medium for detecting Cherenkov radiation from the charged particles left after a neutrino collides with a nucleus.

Many models predict a flux of neutrinos from diffuse extragalactic sources (such as active galactic nuclei). In this work, a search is performed in data taken during the austral winter of 2000 by the AMANDA detector. The search finds 4 events on a predicted background of 3.26 events. Therefore, for an assumed $E^{-2}$ spectrum a $90 \%$ classical confidence belt upper limit on the flux is set at $4.8 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$ for neutrinos in the energy range $12-2000 \mathrm{TeV}$. This is currently the most stringent limit placed on this flux by any experiment.

To Mom and Dad who inspired me to dream.

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## Chapter 1

## Introduction

Mankind has long looked with curiosity at the night sky. Stars and planets provided not only a source of myths, but also served as valuable navigational tools. This is likely the reason astronomy is among the oldest of sciences.

Up until the turn of the twentieth century, the only means of observing the sky was with photons at optical wavelengths. During the twentieth century photon astronomy expanded to new wavelengths. Modern astronomy looks at the sky in every band from radio waves to gamma rays. These new ways of seeing the universe paved the way for discovery. New objects and undreamed phenomena, such as pulsars, active galaxies, gamma ray bursts, and more were revealed.

A defining development for astronomy came in 1912 when Victor Hess discovered cosmic rays. This led to the use of protons and other nuclei as messengers from space. These new messengers brought with them a whole host of questions such as concerning their origin and the mechanism that accelerates them. These questions still puzzle scientists today.

In the past decades a new particle, the neutrino, has lent itself to probing
solutions to these questions. As messengers from space, neutrinos have advantages over photons and cosmic rays since they are not absorbed or deflected at high energies. The distance a photon can travel through space falls quickly at PeV energies as its mean free path length is limited to the Mpc scale [1] while cosmic rays are deflected by magnetic fields as they travel through space.

The idea of using oceans as sites for large neutrino detector date back to the 1960s [2, 3, 4]. Early attempts to use neutrinos as messengers from space started with the DUMAND project [5] in 1975. At the time of this thesis, there were three operational neutrino telescopes (ANTARES, AMANDA-II, and Baikal) and two neutrino telescopes in the development and prototyping stage, IceCube and NESTOR.

Much time and care has gone into understanding how to calibrate and analyze the data from the AMANDA experiment. These analyses have been the topic of many theses and papers. The first result, a glimpse of the atmospheric neutrino spectrum as seen by the AMANDA detector, was published in a letter to Nature in 2000 [6]. Since that time, AMANDA has further established itself as a landmark scientific experiment and has published results of analyses on neutrino point sources [7], diffuse flux muon and electron neutrinos [8, 9], WIMPs [10], and supernova [11].

This work has helped to pave the way for the topic of this thesis: the first search for muon neutrinos from diffuse astronomical sources with the AMANDA-II detector.

## Chapter 2

## High Energy Neutrino Physics and

## Astrophysics

### 2.1 Cosmic Rays

Cosmic rays are perhaps one of the oldest, most puzzling creatures known to Man. They are known to consist of mostly protons and also heavier atomic nuclei, yet their origin is not yet fully understood. However, it is clear that nearly all cosmic rays come from outside the solar system, but from within the galaxy. The most prevalent theory is that most cosmic rays are accelerated by supernovae explosions. The case for supernovae explosions is strengthened by the realization that the first order Fermi acceleration at a strong shock naturally produces a spectrum of cosmic rays consistent with what is observed.

The energy spectrum of cosmic rays is well described by the power-law

$$
\begin{equation*}
\frac{d N}{d E} \propto E^{-\alpha} \tag{2.1}
\end{equation*}
$$

where $\alpha$ is the spectral power index. The value of the spectral index is constant
at $\alpha=2.7$ for most energies. However, around 3 PeV , the region known as "the knee", the slope steepens to a value of $\alpha=3.0$. Observations above 5 EeV , the region known as "the ankle", indicate a flatter spectrum. Figure 2.1 shows the differential energy spectrum of cosmic rays.

The same engines that produce the highest energy cosmic rays may also produce neutrinos. Hence, the search for the origin of the highest energy cosmic rays and the search for high energy neutrinos are intimately related.

### 2.1.1 Fermi Acceleration

Fermi acceleration $[13,14]$ is commonly accepted as the most plausible explanation for the particle acceleration as it can reproduce the observed spectrum of cosmic rays. The acceleration of particles to non-thermal energies takes place in supersonic shock waves. These accelerated particles are theorized to be present in supernovae, jets produced by active galactic nuclei (AGN), and other violent astronomical objects.

Particles gain energy in Fermi acceleration through the transfer of kinetic energy from shocked material in repeated "encounters" with the material. Firstorder Fermi acceleration describes the interaction of particles with a plane shock front, while second-order Fermi acceleration describes interactions of particles with moving clouds of plasma. These scenarios are illustrated in Fig. 2.2 and Fig 2.3. The main difference between the two cases is that in second-order Fermi acceleration particles can gain or lose energy in a given encounter. However, after many encounters there is a net gain in second-order Fermi acceleration. The


Figure 2.1: The cosmic ray spectrum adapted from [12].


Figure 2.2: First order Fermi acceleration by a plane shock front. Adapted from [15].


Figure 2.3: Second order Fermi acceleration by moving, partially ionized gas cloud. Adapted from [15].
following derivation for first-order Fermi acceleration follows that given in [15].
Consider a relativistic particle with energy $E_{1}$ that encounters a plane shock front at an angle $\theta_{1}$ as shown in Fig 2.2. In the rest frame of the shock, the particle has an energy

$$
\begin{equation*}
E_{1}^{\prime}=\Gamma E_{1}\left(1-\beta \cos \theta_{1}\right) \tag{2.2}
\end{equation*}
$$

where $\Gamma$ and $\beta \equiv V / c$ are the Lorentz factor and velocity of the shock respectively and the primes denote the quantities measured in the frame moving with the
shock. Transforming the energy to the rest frame of the particle gives

$$
\begin{equation*}
E_{2}=\Gamma E_{2}^{\prime}\left(1+\beta \cos \theta_{2}^{\prime}\right) \tag{2.3}
\end{equation*}
$$

Since magnetic fields in the shock field produce elastic scattering, $E_{2}^{\prime}=E_{1}^{\prime}$. Thus, the energy change, $\Delta E$, for the encounter described by $\theta_{1}$ and $\theta_{2}$ is given by

$$
\begin{equation*}
\frac{\Delta E}{E_{1}}=\frac{1-\beta \cos \theta_{1}+\beta \cos \theta_{2}^{\prime}-\beta^{2} \cos \theta_{1} \cos \theta_{2}^{\prime}}{1-\beta^{2}}-1 \tag{2.4}
\end{equation*}
$$

Averaging over $\cos \theta_{1}$ and $\cos \theta_{2}^{\prime}$ gives $\Delta E \sim(4 / 3) \beta E_{1}=\epsilon E_{1}$. Thus, a particle encountering a shock increases its energy in proportion to its original energy. After $n$ encounters, the particle's energy is given by

$$
\begin{equation*}
E_{n}=E_{0}(1+\epsilon)^{n} \tag{2.5}
\end{equation*}
$$

where $E_{0}$ is the energy of the particle before the encounter. The number of particles to reach an energy $E$ is then given by

$$
\begin{equation*}
n=\frac{\log \frac{E}{E_{0}}}{1+\epsilon} . \tag{2.6}
\end{equation*}
$$

If the probability of particles escaping the acceleration region is given by $P_{e s c}$, then after $n$ encounters the escape probability is given by

$$
\begin{equation*}
P_{n}=\left(1-P_{e s c}\right)^{n} . \tag{2.7}
\end{equation*}
$$

The number of particles accelerated to energies greater than $E$ is then

$$
\begin{equation*}
N(>E) \propto \sum_{m=n}^{\infty}\left(1-P_{e s c}\right)^{m}=\frac{\left(1-P_{e s c}\right)^{n}}{P_{e s c}} \tag{2.8}
\end{equation*}
$$

Substituting $n$ gives

$$
\begin{equation*}
N(>E) \propto \frac{1}{P_{\text {esc }}}\left(\frac{E}{E_{0}}\right)^{-\gamma} \tag{2.9}
\end{equation*}
$$

where

$$
\begin{equation*}
\gamma=\frac{\log \frac{1}{1-P_{e s c}}}{\log 1+\epsilon} \tag{2.10}
\end{equation*}
$$

For a differential spectrum equation 2.9 takes the form

$$
\begin{equation*}
\frac{d N}{d E} \propto \frac{1}{\gamma} \frac{1}{P_{\text {esc }}}\left(\frac{E}{E_{0}}\right)^{-(\gamma+1)} \tag{2.11}
\end{equation*}
$$

As shown in [15] for shock fronts the spectral index can be approximated as

$$
\begin{equation*}
\gamma=1+\frac{4}{M^{2}} \tag{2.12}
\end{equation*}
$$

where $M=$ the Mach number $\gg 1$. In this case, the spectral index tends to $\gamma \sim 1$ which corresponds to a differential index of $(\gamma+1) \sim 2$ at the source. Neutrinos that result from Fermi accelerated protons/pions are expected to have this energy spectrum, $E^{-2}$, when they reach the earth.

This simplified derivation uses the test particle assumption, meaning the particles being accelerated did not affect the conditions in the acceleration region. More detailed calculations can result in $\gamma \approx 2.0-2.4$. Taking into account the known energy-dependent leakage of cosmic rays out of the galaxy modifies the spectrum by $\delta \gamma$ of 0.3 to 0.6 . This leads to a final spectral index for first order Fermi accelerations is $\gamma \sim 2.7$ for cosmic rays [15].

### 2.2 Neutrinos as a Source of Information

The universe has been explored throughout the electromagnetic spectrum, from radio waves to high energy gamma rays. However, it has not been until recently that we have been able to examine the universe with a new particle, the neutrino.

The advantages of using neutrinos as information carriers is demonstrated in Fig. 2.4. Foremost, neutrinos are not absorbed at high energies by ambient matter or photon fields like their photon counterparts. Photon absorption happens at the Mpc scale [1] and is the limiting adversary faced by gamma ray astronomy. Secondly, unlike cosmic rays, which are deflected by magnetic fields as they travel through space, neutrinos always point directly back to their source.

Astrophysical sources produce high energy gamma rays primarily by radiative processes from accelerated electrons, such as Compton scattering and synchrotron radiation, as well as the decay of pions:

$$
\begin{align*}
p+\gamma \longrightarrow p+ & \pi^{0}  \tag{2.13}\\
& \longmapsto 2 \gamma .
\end{align*}
$$

In contrast, neutrinos are produced via hadronic processes. The primary sources of these neutrinos are through the decay of pions and kaons:

$$
\begin{align*}
p+X \longrightarrow & \pi^{ \pm}+Y \\
\longmapsto & \mu^{ \pm}+\nu_{\mu}\left(\overline{\nu_{\mu}}\right)  \tag{2.14}\\
& \longmapsto e^{ \pm}+\nu_{e}\left(\bar{\nu}_{e}\right)+\bar{\nu}_{\mu}\left(\nu_{\mu}\right)
\end{align*}
$$



Figure 2.4: Neutrinos can travel from greater distances than photons because they are not absorbed by ambient matter or photon fields. Furthermore, neutrinos are not deflected by magnetic fields and always point directly back to their source, unlike cosmic rays [16].

$$
\begin{align*}
p+X \longrightarrow & K^{ \pm}+ \\
\longmapsto & \mu^{ \pm}+\nu_{\mu}\left(\bar{\nu}_{\mu}\right)  \tag{2.15}\\
& \longmapsto e^{ \pm}+\nu_{e}\left(\bar{\nu}_{e}\right)+\bar{\nu}_{\mu}\left(\nu_{\mu}\right)
\end{align*}
$$

$$
p+X \longrightarrow K_{L}^{0}+Y
$$

$$
\begin{equation*}
\longmapsto \pi^{ \pm}+\mu^{ \pm}+\nu_{\mu}\left(\bar{\nu}_{\mu}\right) . \tag{2.16}
\end{equation*}
$$

$$
\longmapsto \pi^{ \pm}+e^{ \pm}+\nu_{e}\left(\bar{\nu}_{e}\right)
$$

Hence, high energy astronomy has the ability to differentiate between hadronic and electronic models of gamma ray emitters such as supernovae remnants, gamma ray bursts, or active galactic nuclei.

### 2.3 Expected Sources of Astronomical High Energy Neutrinos

### 2.3.1 The Atmosphere

Atmospheric neutrinos are produced in abundance in Earth's upper atmosphere. These neutrinos have energies that span a few MeV up to the highest energy cosmic rays. They serve as both a background and calibration beam in the search for extraterrestrial neutrinos.

Cosmic rays constantly bombard Earth's atmosphere, producing extensive air-showers when they interact with nuclei in the air. At the energies relevant to the AMANDA detector, cosmic rays consist of protons and helium nuclei with
some contributions from heavier nuclei. The spectrum of cosmic rays follows a power law, $E^{-2.7}$, in the energy range of interest for AMANDA.

Cosmic ray nuclei interact producing new particles, such as pions and kaons. Neutrinos arise primarily from the decay of these pions and kaons as described by equations $2.14-2.16$. These neutrinos are referred to as atmospheric neutrinos because of their origin. The atmospheric neutrino spectrum follows a power law of $E^{-3.7}$, which is steeper than that of the cosmic rays they come from as shown in fig 2.1. The reason for this is that at high energies, pions tend to interact more often than they decay.

Another reaction that can create neutrinos in the atmosphere is the decay of charm particles, primarily D mesons. Charmed particles have a short lifetime. Consequently, the neutrinos that arise from these decays are referred to as prompt neutrinos. Prompt neutrinos constitute only a few percent of the neutrino flux at 1 TeV and become a dominant source of neutrinos in the atmosphere only at higher energies. The precise energy and flux of prompt neutrinos is heavily model-dependent.

Although the angular distribution of cosmic rays is isotropic, the spectrum of atmospheric neutrinos is dependent on zenith angle. Near the horizon the flux is more prominent. This is because pions, kaons, and muons produced nearly tangent to Earth have longer flight times through the atmosphere. Thus, they have more of a chance to decay into neutrinos. The effect is seen as a symmetric peak in zenith angle about the horizon in Fig 2.5.


Figure 2.5: The atmospheric neutrino spectrum has a symmetric peak about the horizon.

### 2.3.2 The Galactic Disk

Galactic neutrinos are produced through the hadronic interactions that happen when cosmic rays diffuse though the interstellar medium. Most of the energy lost in these interactions goes into the production of mesons. These mesons subsequently decay into gamma rays and neutrinos. Since there is no atmosphere in the galactic disk, most of the mesons produced decay into neutrinos. Hence, the spectrum of gamma rays and neutrinos resembles that of the cosmic ray spectrum in the interstellar medium, $\frac{d N}{d E}=E^{-2.7}$. The flux of galactic neutrinos is small and they have a steep spectrum. Thus, they only become an issue above 1 PeV (see Fig. 2.7). Even then, the AMANDA detector's location at the south pole makes galactic neutrino detection challenging. Thus, they pose no background to this analysis.

### 2.3.3 Active Galactic Nuclei (AGN)

One promising source of extragalactic neutrinos is active galactic nuclei (AGN). AGN are among the most energetic objects in the universe. They emit as much energy as an entire galaxy, but are extremely compact. Their luminosities have been observed with flares extending over periods of days. The frequency of the flaring can vary from hours to years. All wavelengths of radiation from radio waves to TeV gamma rays are emitted from AGN.

AGN are believed to be powered by accreting super-massive black holes lurking in the centers of galaxies. There are two generic models for neutrino production in AGN: core models and jet models. The main difference in these
models is where the neutrinos are produced.
In core models, the neutrinos are believed to be produced in Fermi shocks of protons inside the accretion disk. The shocked protons interact with protons or photons in and around the disk producing neutrinos though pion decay as demonstrated in equation 2.14.

In AGN jet models some of the in-falling matter from the accretion disk is believed to be re-emitted and accelerated in highly energetic beamed jets that are aligned with the axis of rotation of the black hole as shown in Fig 2.6.

The particles in the relativistic jet are assumed to be accelerated by Fermi shocks in clumps or sheets of matter traveling along the jet with Lorentz factors of 10-100.

Gamma rays can be produced from electron acceleration by synchrotron radiation or Compton scattering. In the case of proton acceleration, the thermal ultraviolet photons or synchrotron photons provide the dominant target for pion production. These pions subsequently decay to gamma rays and neutrinos via equation 2.14. Different neutrino spectra are expected from electrons and photons and are the subject of debate. An observation of high energy neutrinos from these sources would help resolve the issue of particle acceleration.

### 2.3.4 Gamma Ray Bursts (GRB)

Gamma Ray Bursts (GRBs) are the most luminous cataclysmic phenomena in the universe. They can be characterized by their flares, which last from a few milliseconds to a few seconds and have short rise times on the order of a


Figure 2.6: Possible production mechanism for AGN. Electrons and possibly protons, which are accelerated in sheets or blobs along the jet, interact with photons that are radiated by the accretion disk or produced in the magnetic field of the jet. Taken from [17].
millisecond followed by an exponential decay. GRBs are randomly distributed across the sky.

Although the powering process behind a GRB is still unknown, the short rise time indicates that they originate from compact objects with diameter of tens of kilometers. Possible sources of such objects are hyper-novae which result from the fusion of neutron stars or super-massive star collapse.

The bursts are believed to be produced by the dissipation of the kinetic energy of a relativistically expanding fireball. Gamma rays could be produced by the decay of neutral pions or emission of synchrotron radiation (possibly followed by inverse Compton scattering) by relativistic electrons accelerated in the dissipation shocks.

In this model, the ultra-relativistic expansion of electron-positron plasma forms a shock wave. Protons may also be accelerated by Fermi acceleration in the same region the electrons are accelerated. Neutrinos would then be created by photo-meson production of pions in interactions between the fireball $\gamma$-rays and accelerated protons.

It is interesting to note that the energy released in a GRB is about the same needed to produce the highest energy cosmic rays, whose origin are still unknown.

### 2.3.5 Exotic Phenomena

The highest energy cosmic rays observed have energies above 100 EeV and are difficult to explain using conventional Fermi acceleration models of charged particles. Some models $[18,19]$ suggest that these ultra-high energy cosmic rays
are produced by the decay of super-massive "X" particles released from topological defects, such as cosmic strings and monopoles, created in cosmological phase transitions. "X" particles can be particles such as gauge or Higgs bosons or superheavy fermions. These particles typically decay into a lepton and a quark. The quark is then theorized to hadronize into nucleons and pions. The pions can then decay into photons, electrons, and neutrinos.

### 2.4 Diffuse Source

The most obvious way to search for the neutrino sources described above is to identify excesses of neutrinos coming from particular sources in the sky. However, individual sources of high energy neutrinos may not be bright enough to be resolved by the AMANDA-II telescope. Fortunately, there are a large number of sources. Thus, the sources produce an isotropic background of neutrinos with high energies. A large neutrino detector, such as AMANDA-II is sensitive to diffuse fluxes of neutrinos from unresolved sources. A measurement of this background could be the first evidence of neutrinos from hidden sources.

Searching for neutrinos from diffuse sources, which is the topic of this work, is much more difficult than looking for a particular point source in the sky as there is no directional information. However, high energy neutrinos predicted to come from diffuse sources have a much shallower energy spectrum, $\left(E^{-2}\right)$, than the atmospheric neutrino background, $\left(E^{-3.7}\right)$.

Theoretical bounds can be made on the diffuse flux of neutrinos from knowl-
edge of the diffuse flux of gamma rays and cosmic rays. In the case of proton acceleration, gamma rays and neutrinos are produced in parallel. Despite the fact that neutrinos escape the source with no further interactions while the gamma rays cascade to lower energies in the source or scatter with the cosmic infrared background, the integral energy of these particles is the same within a factor of two [21]. The EGRET experiment[20] aboard the Compton Gamma Ray Observatory measured the isotropic diffuse gamma ray background intensity as

$$
\begin{equation*}
\Phi(E>30 \mathrm{MeV})=(1.37 \pm 0.06) \times 10^{-6} E^{-2.1 \pm 0.03} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV} \tag{2.17}
\end{equation*}
$$

Taking into account the factor of two mentioned above, the upper theoretical bound of the neutrino flux is on the order of $10^{-6} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$. This limit can be seen in figure 2.7 as the straight upper boundary of the extragalactic region.

A similar argument can be made for sources where both gamma-ray and cosmic-ray nucleons escape. For an optically thick source, both protons and neutrons are trapped in the source and the gamma ray limit applies. However, for optically thin sources, it is possible for the neutrons to escape the source without energy loss and inversely $\beta$-decay into cosmic protons outside the source. These neutrons then travel unaffected by magnetic fields in the Universe. The neutrino upper bound for these sources is represented by the curved upper boundary of the extragalactic region in figure 2.7.


Figure 2.7: Expected fluxes of $\nu+\bar{\nu}$ intensities for emission from various diffuse sources taken from [21]. Fluxes 1-2 are predicted using the core model of emission from AGNs [22, 23], while fluxes 3-6 use the AGN jet (blazar) model [24, 25, 26, 27]. Flux 7 is a prediction of neutrinos from GRBs [28], while flux 8 is a neutrino prediction from topological defects [18, 19].

### 2.5 Neutrino Oscillations

Evidence from GeV scale atmospheric and MeV solar neutrino experiments, Super-Kamiokande [29] and Sudbury Neutrino Observatory (SNO) [30] strongly suggest that neutrinos oscillate from one flavor to another. The LSND accelerator experiment has also reported observing large neutrino oscillations [31]. This result is controversial and experiments are under way to confirm or refute it. In order to accommodate all three experiments a fourth neutrino, the sterile neutrino $\left(\nu_{s}\right)$, which does not interact has been postulated. The following discussion will consider the simplified case of two-flavor oscillations.

In order for neutrinos to oscillate from one flavor to another, neutrinos must be massive, and the eigenstates for weak interactions must be different than those for free neutrinos. The probability of a neutrino of flavor $\ell$ and energy $E_{\ell}$ that travels a distance L in vacuum to oscillate to a neutrino of flavor $\ell$, is given by

$$
\begin{equation*}
P_{\nu_{\ell} \nu_{\ell}}=\sin ^{2} 2 \theta \sin ^{2} \pi \frac{L}{L_{o s c}} \tag{2.18}
\end{equation*}
$$

where $\sin ^{2} 2 \theta$ is the mixing angle between the two neutrinos and $L_{\text {osc }}=4 \pi E_{\ell} / \Delta m^{2}$ is the oscillation length in vacuum.

At their source, neutrinos are produced in the ratio $\nu_{e}: \nu_{\mu}: \nu_{\tau} \sim 1: 2: 0$. Due to oscillations as they travel through space, the ratio observed at Earth is $1: 1: 1$ [32]. Thus, muon neutrino fluxes predicted at their source would on Earth be observed as one-half the predicted flux at the source. This should be kept in mind when interpreting analysis results as many diffuse spectrum flux theories do not take this into account.

## Chapter 3

## Detection of Neutrinos

### 3.1 Neutrino-Nucleon Interactions

It is well known that neutrinos can not be directly detected. However, a neutrino or anti-neutrino traveling through matter has some small probability of interacting through charged-current scattering

$$
\begin{align*}
& \nu_{l}+N \rightarrow l^{-}+X  \tag{3.1}\\
& \bar{\nu}_{l}+N \rightarrow l^{+}+X \tag{3.2}
\end{align*}
$$

where $l$ is the lepton flavor, $N$ is the target nucleon, and X is a combination of final state hadrons. At high energies, the lepton carries approximately half the energy of the neutrino. From the kinematics of this reaction, the neutrino and the lepton will be collinear to a mean deviation of

$$
\begin{equation*}
\sqrt{\left\langle\theta_{2}^{\mu \nu}\right\rangle} \approx \sqrt{m_{p} / E \nu} \tag{3.3}
\end{equation*}
$$

which is about 1.75 degrees for a 1 TeV neutrino. The other half of the energy is released in the hadronic cascade, $X$, producing a bright, relativity localized flash
of light.
The cross section for the charged-current neutrino-nucleon interaction in the rest frame of the nucleon (assuming a relativistic outgoing lepton) is [33]

$$
\begin{equation*}
\frac{d^{2} \sigma}{d x d y}=\frac{2 G_{F}^{2} M_{N} E_{\mu}}{\pi}\left(\frac{M_{W}^{2}}{Q^{2}+M_{W}^{2}}\right)\left[x q\left(x, Q^{2}\right)+x \bar{q}\left(x, Q^{2}\right)\left(1-y^{2}\right)\right] \tag{3.4}
\end{equation*}
$$

where $-Q^{2}$ is the invariant momentum transfer from the neutrino to the outgoing muon, $q$ and $\bar{q}$ are the parton distribution functions of the nucleon, $G_{F}$ is the Fermi constant for weak interactions and $M_{N}$ and $M_{W}$ are the masses of the nucleon and W boson. The Bjorken scaling variables, $x$ and $y$, are given by

$$
\begin{equation*}
x=\frac{Q^{2}}{2 M_{N}\left(E_{\nu_{l}}-E_{l}\right)} \tag{3.5}
\end{equation*}
$$

and

$$
\begin{equation*}
y=1-\frac{E_{l}}{E_{\nu_{l}}}, \tag{3.6}
\end{equation*}
$$

where $x$ is the fraction of the nucleon's four-momentum carried by the interacting quark and $y$ is the fraction of the neutrino's energy deposited in the interaction. At low energies, the neutrino cross section is four times greater than that of the antineutrino and the cross section is dominated by interactions with valence quarks. However, at high energies their cross sections become equal as they predominantly interact with sea quarks in the nucleon, shown in Fig 3.1.

At low energies, $-Q^{2} \ll M_{W}$, and the term in parentheses in equation 3.4 can be neglected. In this region, the neutrino-nucleon cross section rises linearly with the neutrino energy. However, when $Q^{2}$ becomes comparable to $M_{W}$, the cross section grows more slowly, as seen in Figs. 3.3 and 3.2. This transition occurs


Figure 3.1: Charged-current neutrino cross sections as a function of energy [33]. The solid line is based on the CTEQ3 parton distributions. The dashed and dotted lines are from older measurements.


Figure 3.2: Differential cross section for neutrino-nucleon scattering for neutrino energies between $10^{4} \mathrm{GeV}$ and $10^{12} \mathrm{GeV}$ from [33].
at approximately 3.6 TeV . In this same region the average value of y begins to fall which leads to an increase in the momentum transfer to the muon and, hence, a longer muon range. The longer muon range helps offset the slower growth in neutrino cross section.

### 3.2 Lepton Signatures

After a neutrino interacts with a nucleon it produces one of three different leptons. Each of these leptons leaves a distinct signature in neutrino detectors. Below the critical energy of about 600 GeV , secondary muons from muon neutrinos deposit their energy continuously at a rate of $\sim 0.2 \mathrm{GeV}$ per meter as they travel in a nearly straight line through the detector. The resulting experimental signature is a long linear deposition of light due to Cherenkov radiation, described in section


Figure 3.3: Energy dependence of the average in-elasticity of neutrino-nucleon interactions from [33].
3.3.1, that leaves a track with length of hundreds of meters, kilometers, or even tens of kilometers, depending on the initial energy of the muon. A typical muon signature in the AMANDA detector is shown in Fig. 3.4.

The signature for an event produced by interactions from an electron neutrino is a bright, spherical deposition of Cherenkov light generated by an electromagnetic cascade, and is shown in Fig. 3.5. Unlike muons, which have a long range, electrons quickly dissipate their energy by radiative processes such as bremsstrahlung and pair production. The electromagnetic cascade reaches its maximum after a few meters, a small distance compared to the spacing of the optical modules. Thus, an electron-neutrino event in the AMANDA detector looks like a point source of light.

The most striking lepton signature, not seen in AMANDA due to the detector's small size, is that of the tau neutrino. When a tau neutrino interacts with a nucleon, it produces a tau particle and a hadronic cascade at its interaction point. Subsequently, the tau particle will travel some distance and decay. This decay


Figure 3.4: A muon event in the AMANDA detector. As the muon passes through the detector, light is emitted at a constant rate.

will produce a second hadronic cascade. This cascade is very difficult to resolve from the first, making it indistinguishable from a cascade produced by an electron, except at very high energies where the tau may travel hundreds of meters. For events that are contained within the detector, this "double bang" topology is a very distinctive signature, as seen in Fig. 3.6.

### 3.3 Muon Energy Loss

### 3.3.1 Cherenkov Radiation

A charged particle moving through a transparent medium with refractive index $n>1$ with speed $v>c / n$ will produce Cherenkov radiation. Cherenkov radiation is emitted at an angle of

$$
\begin{equation*}
\cos \theta_{C}=\frac{1}{\beta n} \tag{3.7}
\end{equation*}
$$

For energies relevant to AMANDA, $\beta \sim 1$. The refractive index of ice is $n=1.34$. Substituting these values into equation 3.7 yields

$$
\begin{equation*}
\Theta_{c}=41^{\circ} \tag{3.8}
\end{equation*}
$$

The energy loss due to Cherenkov radiation is $\sim 10^{3} \mathrm{MeV} / \mathrm{cm}$, relatively small compared to the total ionization loss of approximately $2 \mathrm{MeV} / \mathrm{cm}$ for minimally ionizing particles [35]. Nonetheless, a muon emits $\sim 200$ photons $/ \mathrm{cm}$, which is enough for detection [36].

Figure 3.6: A tau event in the future IceCube detector. The two cascades of light are produced by the initial neutrino-nucleon interaction and subsequent decay of the tau particle.

### 3.3.2 Stochastic Energy Deposition

Muons can lose energy through several mechanisms: ionization, bremsstrahlung, pair production, and photo-nuclear processes. Ionization is a quasi-continuous process and can be treated continuously, while the others are stochastic in nature. The average rate of stochastic energy loss is nearly proportional to the muon energy. The total rate of energy loss of a muon traveling through ice per unit length can be parameterized by

$$
\begin{equation*}
-\frac{d E_{\mu}}{d x}=a\left(E_{\mu}\right)+b(E \mu) \cdot E_{\mu} \tag{3.9}
\end{equation*}
$$

where $a$ is the energy loss due to ionization and $b \cdot E$ is the energy loss due to stochastic processes [34].

In ice the value of $a$ is approximately $0.2 \mathrm{GeV} / \mathrm{m}$ [34] and value of $b$ is approximately $3.4 \times 10^{-4} \mathrm{~m}^{-1}$. Thus, stochastic events are the main component of energy loss for muons above 600 GeV .

## Chapter 4

## The AMANDA Detector

AMANDA (the Antarctic Muon and Neutrino Detector Array) is an ice Cherenkov telescope located beneath the ice at the Amundsen-Scott South Pole Station. The detector is an array of 677 photomultiplier tubes and was built over the course of five years. Its primary mission is the detection of neutrinos originating from astrophysical sources.

### 4.1 History

The first effort to build an under-ice neutrino detector was in the austral summer of 1993/94. Four strings, each with 20 optical modules, were deployed at depths between 800 and 1000 meters. This detector became known as AMANDAA. Studies of the ice properties at these depths showed the absorption length to be around 200 meters at the peak absorption of the photomultiplier tubes (PMTs) of 400 nm . At the same time, the scattering length was on the order of $10-20 \mathrm{~cm}$, a value too small to allow the reconstruction of muon trajectories. The scattering length was dominated by tiny air bubbles trapped in the ice. It was thought
that these bubbles would be absent at 800 m as a result of the phase transition that occurs as the increasing pressure transform the air bubbles into air hydrate crystal. However, due to the low temperatures at the south pole, the diffusion of air molecules into the ice crystalline structure slows down. Thus, the bubbles only completely disappear at about 1300 m [37].

Learning from the experiences with the AMANDA-A array, the 19 strings of AMANDA-II were deployed at greater depths (1500m-2000 m) in stages during the austral summers from 1995-2000.

### 4.2 The Detector

The AMANDA detector consists of a three-dimensional array of optical modules (OMs). Each OM consists of an 8" Hamamatsu PMT housed in a glass pressure sphere. The OMs are connected to the surface by an electrical cable which serves two purposes. The cable provides the high voltage necessary to operate the PMT and transmits signals from the PMTs back to the data acquisition (DAQ) system electronics at the surface.

As the AMANDA detector grew through years of deployment, the hardware used to construct the detector matured. The first 4 strings of what is now known as the AMANDA detector (then called AMANDA-B4) were deployed in the austral summer of 1995-96. These 86 OMs where connected to the surface by coaxial cable, which provided protection against electronic crosstalk in the cables. Unfortunately, coaxial cable has limitations. Coaxial cable is quite dispersive, resulting
in distortion during the course of transmission to the surface (10 ns PMT pulses arrive at the surface with a width of more than 400 ns ). Coaxial cable is also quite thick, limiting the number of cables that could be bundled together.

For these reasons the next 6 strings, which were deployed during the austral summer of 1996-97, used twisted pair cables. These 6 strings brought the total number of OMs in the array to 302. This new array was named AMANDA-B10. The twisted pair cables had less dispersion (150 ns - 200 ns ) and allowed more cables per string. However, a great deal of electronic crosstalk was observed in these strings.

During the austral summer of 1997-98 another 3 strings were deployed bringing the total number of OMs to 428. These strings had both optical fibers and traditional twisted pair cables. The optical fibers were essentially dispersion free and crosstalk free. However, they were quite fragile and nearly $10 \%$ were damaged during the refreeze process. Another change in the deployment of these three strings was that they were to lie at a depth between $1200 \mathrm{~m}-2400 \mathrm{~m}$ in order to study the optical properties above and below the detector.

The last strings to be added to the array were strings 14-19 in the austral 1999-2000 summer. This marked the completion of the AMANDA-II detector. All OMs on these strings were connected to the surface via optical fibers and traditional twisted pair cables. Some of the modules deployed during this year contained experimental digital technologies under investigation for future iceCherenkov detectors. String 18 is comprised entirely of digital optical modules


Figure 4.1: Top view of the AMANDA-II detector. The radius of the detector is approximately 100 meters.
(DOMs). These modules contained analog transient waveform digitizers (ATWDs) which record and digitize the signal in situ and then transmit them to the surface. This technology results in the full retention of waveform information without the need for optical fibers. However, the DAQ electronics are buried with the OMs in the ice, hence, beyond the possibility of repair or upgrade.

The complete AMANDA-II detector contains 19 strings, 677 OMs and instruments $0.015 \mathrm{~km}^{3}$ of ice. It has a diameter of 200 m and a height of 500 m . The modules on each string are separated by $10 \mathrm{~m}-20 \mathrm{~m}$, depending on the string. The strings are arranged in three concentric circles and separated by $30 \mathrm{~m}-60$ m. Figures 4.1 and 4.2 show the layout of the AMANDA detector.


Figure 4.2: Schematic of the geometry of AMANDA-II. AMANDA-A and AMANDA-B10 are shown in expanded view in the center. An optical module is blown up on the right. The Eiffel Tower is shown to illustrate the scale.

The first strings of the IceCube detector are scheduled to be deployed in the austral summer of 2004-05. The entire IceCube array will contain some 4800 OMs, 80 strings and instrument $1 \mathrm{~km}^{3}$ of ice. It is scheduled to be completed in 2009-10. All of the OMs in the IceCube array will use the DOM technology. IceCube will be deployed between the depths of 1400 m and 2400 m .

### 4.3 Data Acquisition

The AMANDA detector trigger can come from a variety of sources. In normal mode, the detector is triggered by the detection of photons by a set number of OMs in a preset window of time (majority trigger). For the AMANDA-II year 2000 data set, 24 OMs were required to receive at least 1 photo-electron in a $2.1 \mu \mathrm{sec}$ time period. The trigger rate was approximately 100 Hz .

The data acquisition (DAQ) system, located on the surface, is responsible for reading out event information and storing it to disk. Information read and stored by the DAQ includes the leading edge time (LE) and the width or time-over-threshold (TOT) in the time window $\sim 22 \mu \mathrm{sec}$ before and $\sim 10 \mu \mathrm{sec}$ after the trigger time. The DAQ also records the amplitude of pulses arriving from the OMs. The analog digital converter (ADC) information is recorded during a time window of $\pm 2 \mu \mathrm{sec}$ around the trigger time. The event time is obtained from a Global Positioning System (GPS) unit.

A majority trigger in AMANDA is formed based on hit multiplicity. When an OM detects a photo-electron it sends a pulse to the surface where it is received
by a Swedish Amplifier (SWAMP) which amplifies the signal. A copy of the signal is then sent to discriminators where the signal is converted to a $2 \mu \mathrm{sec}$ square pulse. The discriminator sends its output to the Digital Multiplicity Adders (DMAD) where multiple signals are summed and compared to a preset threshold. In 2000, this threshold was set at 24 channels. When the sum crosses the threshold, a stop signal is sent to all time digital converters (TDCs) and a veto of several $\mu$ sec is sent to the trigger. All channels are then read out and the system reset.

### 4.4 Ice Properties

Understanding the properties of the ice is crucial for the operation of the AMANDA-II detector. Thus, the scattering and absorption properties, which affect the timing and number of photons that reach the OMs, must be throughly understood. Numerous studies using both in-situ light sources and atmospheric muons have been conducted to determine the ice properties.

The ice is characterized using three parameters: the scattering length $\lambda_{b}$ (or the scattering coefficient $b=1 / \lambda_{b}$ ), the absorption length $\lambda_{a}$ (or the absorption coefficient $a=1 / \lambda_{a}$ ), and the average of the cosine of the scattering angle ( $\tau_{s}=$ $\langle\cos \theta\rangle$. The effective scattering length is then defined as $\lambda_{b}^{e f f}=\lambda_{s} /\left(1-\tau_{s}\right)$ and its coefficient is $b_{e}=1 / \lambda_{b}^{e f f}$. The effective scattering and absorption coefficients are shown in Figs. 4.3 and 4.4 as a function of wavelength.

Dust grains (about 0.04 microns in size) are the biggest contributors to scattering and absorption in the antarctic ice below 1400 meters. Air bubbles,


Figure 4.3: Absorption coefficients as a function of depth at various wavelengths [38].
which were the largest scatterers in the AMANDA-A detector, are squeezed into air hydrate crystals which have nearly the same index of refraction as ice at AMANDA-II depths and pose no problems to light detection.

Although the glacial ice in which AMANDA-II is embedded is nearly uniform, climatological events in Earth's past, such as ice ages, have left layers of impurities in the form of dust, soot, etc. These dust layers affect the optical properties of the ice and affect photon propagation.

The first measurements of the scattering and absorption coefficients of these layers was done using a YAG laser at a frequency of 532 nm . Figure 4.5 shows the effective scattering coefficient as a function of depth in the detector. The dust


Figure 4.4: Scattering coefficients as a function of depth at various wavelengths [38].
layers are visible as peaks in the scattering coefficient while the clear layers are visible as valleys.


Figure 4.5: Scattering coefficient as a function of depth, indicating the presence of dust layers. On the left side of the plot the depth of the OMs in relation to the dust layers are shown [39].

## Chapter 5

## Event Reconstruction and Analysis Tools

Reconstruction algorithms in AMANDA, like the hardware used to build it, have developed over time. Reconstructions for both muon tracks and cascades are based on the principle of maximization of a likelihood function. Due to how sparsely the AMANDA detector is instrumented, only a limited set of parameters can be constrained for each event. For muons, these parameters are direction $(\theta, \phi)$, position $(x, y, z)$, and time $(t)$.

### 5.1 Direct Walk Reconstruction

The direct walk [40, 41, 42] method of reconstruction is a first guess method of reconstruction based on pattern recognition of selected hits from photons that have not scattered much in the ice. First guess methods of reconstruction are very fast analytic algorithms that are used as initial track guesses for more complicated algorithms which will be described in the following sections.

The direct walk algorithm looks for track elements which are pairs of hits consistent with a close track such that

$$
\begin{equation*}
\left|\frac{\left|\overrightarrow{r_{1}}-\overrightarrow{r_{2}}\right|}{c}-\left|t_{1}-t_{2}\right|\right|<30 \mathrm{~ns} \tag{5.1}
\end{equation*}
$$

where $\overrightarrow{r_{i}}$ is the position of the $i$ th hit and $t_{i}$ is the time of the $i t h$ hit. Associated hits, those with small time residuals and appropriate distance from the track element based on time residuals, are selected. Quality criteria such as the number of associated hits, the spread of associated hits, and the hit density along the track element are applied. Track elements that pass these criteria are called track candidates. The final first guess track is then found by searching for clusters in zenith angle of track candidates and calculating the mean of all track candidates belonging to the cluster.

### 5.2 Maximum Likelihood Reconstruction

The maximum likelihood method [42] is a generalization of the $\chi^{2}$ method. In the limit of Gaussian uncertainties the likelihood, $\mathcal{L}$, is related to $\chi^{2}$ by $-2 \ln \mathcal{L}=\chi^{2}$. These methods attempt to find the track hypothesis that maximizes the likelihood by minimizing $-\log \mathcal{L}$ with respect to the track parameters. In general, the likelihood for a given event $E_{0}$, which is a collection of detector responses $\mathcal{R}_{i}$ and a hypothesis $H_{j}$, is written as

$$
\begin{equation*}
\mathcal{L}\left(E_{0} \mid H_{j}\right)=\prod_{i} \mathcal{L}_{i}\left(\mathcal{R}_{i} \mid H_{j}\right) . \tag{5.2}
\end{equation*}
$$

If the hypothesis is true, it then generates the observed pattern of hits. The hypothesis is then allowed to vary and an optimization routine is used to find
the location $H_{0}$ of the global extremum of $\mathcal{L}$. The responses $\left\{R_{i}\right\}$ recorded by AMANDA are the time, $t_{i}$, and duration, $T O T_{i}$, of each PMT signal and the peak amplitude, $A_{i}$, of the largest pulse in each PMT.

In the case of muon reconstruction, one assumes that the Cherenkov radiation is generated by a single infinitely long muon track. This is a reasonable assumption for the energies of this analysis which simplifies and speeds up the calculation and optimization. For muons, this reduces the function $H$ to sixdimensions $H=H(\vec{x}, \theta, \phi, t)$.

### 5.2.1 Time Likelihood

By applying the assumption of an infinitely long muon track we arrive at the simplified likelihood function. The function depends on the arrival time of the light,

$$
\begin{equation*}
\mathcal{L}=\prod_{i=1}^{n h i t s} p\left(t_{\text {res }}^{i} \mid d_{i}, \eta_{i} \ldots\right) \tag{5.3}
\end{equation*}
$$

where $t_{\text {res }}^{i}$ is the time delay, $d_{i}$ is the distance of the OM from the track, and $\eta_{i}$ is the orientation of the OM relative to the track. The probability density function of single photons, $p\left(t_{r e s}^{i} \mid d_{i}, \eta\right)$, was generated by parameterizing Monte Carlo simulations of photon propagation in ice [43].

The negative logarithm of the likelihood function, $-\log \mathcal{L}$, is then minimized using a Simplex [44] algorithm in an iterative technique, which performs multiple reconstructions of the same event. Each reconstruction starts with a different initial track hypothesis. The results of all iterations are compared to each other.

The lowest value of $-\log \mathcal{L}$ is taken as the reconstructed track.

### 5.2.2 Bayesian Likelihood

Bayes' theorem allows us to fold in information independent of the measurement into the likelihood function. The theorem states

$$
\begin{equation*}
P(A \mid B) P(B)=P(B \mid A) P(A) \tag{5.4}
\end{equation*}
$$

Identifying $A$ with the hypothesis $H$ and $B$ with the hit pattern $E$ and solving for $P(H \mid E)$ gives

$$
\begin{equation*}
P(H \mid E)=\frac{P(E \mid H) P(H)}{P(E)} \tag{5.5}
\end{equation*}
$$

The quantity $P(E \mid H)$ is the likelihood that the given set of hits would be generated by the hypothesis of interest. $P(E)$ is the probability that a given pattern of hits is observed. This quantity is independent of track parameters and is therefore constant. $P(H)$ is known as the prior and does not depend in any way on the measurement. It is the probability of observing the track and can be calculated prior to the measurement. Thus, $P(H \mid E)$ is the probability of the hypothesis after $E$ is taken into account.

Bayesian event reconstruction [45] uses the prior probability function shown in Fig. 5.1. This function is flat over the up-going hemisphere and dependent on zenith angle in the down-going hemisphere. Reconstructing using this technique requires one to maximize the product of the probability density function and the prior. Similar to the time likelihood reconstruction, this is done using the Simplex minimizer and an interactive minimizing technique.


Figure 5.1: The prior function used is flat over the up-going hemisphere and dependent on zenith angle in the down-going hemisphere [36].

Near the horizon the effect of the Bayesian reconstruction is strongest. Since AMANDA-II is narrow, events coming in near the horizon have shorter track lengths, making it difficult to constrain the fit tightly. The prior indicates that tracks from atmospheric muons are more likely than neutrinos. Thus, the reconstruction properly chooses the down-going fit as being more likely.

### 5.3 Quality Parameters

Quality parameters are used for selection criteria during different stages of the analysis. Below are descriptions of the parameters that will be used for this analysis.

### 5.3.1 Likelihood Ratio

As discussed in the previous section, a Bayesian maximum likelihood fit is performed on the sample to fit muon tracks to the observed events. The functional form used is the negative logarithm of the likelihood. This analysis uses two likelihood ratios, up-to-down and track-to-cascade. The likelihood ratio for up-to-down going events is defined as

$$
\begin{equation*}
R_{L}^{u / d}=\log \left(\frac{\mathcal{L}_{u p}}{\mathcal{L}_{\text {down }}}\right) \tag{5.6}
\end{equation*}
$$

and the likelihood ratio for track-like to shower-like events is defined as

$$
\begin{equation*}
R_{L}^{t / s}=\log \left(\frac{\mathcal{L}_{\text {track }}}{\mathcal{L}_{\text {shower }}}\right) \tag{5.7}
\end{equation*}
$$

$\mathcal{L}_{u p}$ is the likelihood of the track being up-going and hence from a neutrino and $\mathcal{L}_{\text {down }}$ is the likelihood of the track being down-going and hence from a cosmic
ray. $\mathcal{L}_{\text {track }}$ is the likelihood of the event being from a muon and $\mathcal{L}_{\text {shower }}$ is the likelihood of the event being from a cascade.

The up/down likelihood ratio is the most powerful parameter for separating cosmic ray background events (down-going) from signal neutrinos (up-going).

### 5.3.2 Smoothness

"Smoothness" $\left(S_{p h i t}\right)$ is a topological parameter that is defined by the distribution of hits along the track. It measures how consistent the observed pattern of hits is with the hypothesis of constant light emission by a muon.

### 5.3.3 Number of Direct Hits

A "direct hit" occurs when a photon is delayed little by scattering in the ice between production and detection. This delay is measured relative to the predicted arrival time of an unscattered Cherenkov photon emitted from the appropriate point along the track. Different delay windows exist for counting direct hits. For this analysis a hit is considered direct when it arrives in a window of [-15:75] nanoseconds. Thus, $N_{d i r}^{[-15: 75]}$, is defined as the number of direct hits in an event.

### 5.3.4 Track Length

The track length is determined by projecting each of the direct hits onto the reconstructed track and measuring the distance between the first and last hits. In this analysis, two different track lengths were defined. The first uses a stricter direct hit definition than described above. For this track length, the direct hits
are required to arrive in the time window [-15:25] nanoseconds

$$
\begin{equation*}
L_{d i r}^{[15: 25]} \tag{5.8}
\end{equation*}
$$

and the second uses the definition of direct hits from above

$$
\begin{equation*}
L_{d i r}^{[15: 75]} \tag{5.9}
\end{equation*}
$$

where direct hits were required to arrive in the [-15:75] nanosecond window.

### 5.3.5 Zenith Angle

In this analysis, the zenith angle of the best up-going fit and the zenith angle of the best down-going fit are also used in conjunction with the number of direct hits of the best up-going fit and the number of hits of the best down-going fit to remove coincident muon events from cosmic rays.

### 5.3.6 Center of Gravity

The center of gravity $(\overrightarrow{c o g})$ of an event is defined as the mean position of all OMs hit by one or more photons in an event. It is represented mathematically as

$$
\begin{equation*}
\overrightarrow{\operatorname{cog}}=\frac{1}{n c h} \sum_{i=0}^{n c h} \overrightarrow{r_{i}} \tag{5.10}
\end{equation*}
$$

where $n c h$ is the number of OM to receive at least one photon and $\overrightarrow{r_{i}}$ is the distance from the center of the detector to the center of the event.

### 5.4 The Model Rejection Potential

An upper limit on an expected flux can be derived from observation when an experiment fails to detect an expected flux. The method used in this thesis is
the model rejection potential [47]. It uses the method developed by Feldman and Cousins [46] to find the limit. In the Feldman and Cousins method, the upper limit, $\mu$, is a function of the number of observed events, $n_{o}$, and the number of predicted background events, $n_{b}$,

$$
\begin{equation*}
\mu \equiv \mu\left(n_{o}, n_{b}\right) \tag{5.11}
\end{equation*}
$$

The flux limit is then calculated by the formula

$$
\begin{equation*}
\Phi_{C L}=\Phi \times\left(\frac{\mu_{C L}}{n_{s}}\right) \tag{5.12}
\end{equation*}
$$

where $C L$ is the desired confidence level of the calculation, $\Phi$ is the expected flux, and $n_{s}$ is the number of signal events predicted from that flux.

Since the actual upper limit cannot be known until looking at the data, simulations can be used to calculate the expected average upper limit. The average upper limit is the sum of the expected upper limits, weighted by their Poisson probability of occurrence. It can be written mathematically as

$$
\begin{equation*}
\bar{\mu}_{C L}=\sum_{n_{o b s=0}}^{\inf } \mu_{C L}\left(n_{o b s, n_{b}}\right) \frac{\left(n_{b}\right)^{n_{o b s}}}{\left(n_{o b s}\right)!} e^{-n_{b}} . \tag{5.13}
\end{equation*}
$$

Using the average upper limit, one can find the optimal selection criteria for setting the best limit without using the data. When the optimal selection criteria are applied to the Monte Carlo simulations, they will yield the sensitivity of the experiment. Over an ensemble of identical experiments, the strongest constraint on the expected signal flux will correspond to the set of cuts that minimizes the model rejection factor. The model rejection factor is defined by

$$
\begin{equation*}
m r f \equiv \frac{\bar{\mu}_{C L}}{n_{s}} \tag{5.14}
\end{equation*}
$$

where $n_{s}$ is the predicted number of signal events from the expected flux.
The model rejection factor can then be used to find the expected upper limit (the sensitivity) defined by

$$
\begin{equation*}
\bar{\Phi}_{C L}=\Phi \times\left(\frac{\bar{\mu}_{C L}}{n_{s}}\right) . \tag{5.15}
\end{equation*}
$$

The actual experiment is not likely to yield exactly $\bar{\Phi}_{C L}$. This is because the limit in that case will be based on the observed number of events, which is subject to fluctuations in the background in that particular experiment. The sensitivity, which is the average flux upper limit, would give the average value expected over repeated runs of a real experiment.

## Chapter 6

## Data and Monte Carlo Simulations

### 6.1 Live-Time

The total data acquisition time for the year 2000 was 254.2 days. Taking into account the dead time of the data acquisition system, this corresponds to 211.5 days of detector live time. During that time there were a total of 1,444,252,130 triggers registered. Of those triggers, $90.7 \%$ were formed with the majority trigger, which required at least 24 OMs to have fired during the event.

File cleaning was performed to remove problematic files. A problematic file is one that has at least one of the following symptoms

$$
\begin{gather*}
N_{\text {hot }}>5  \tag{6.1}\\
N_{\text {dead }}>50  \tag{6.2}\\
N_{\text {unstable }}>10 \tag{6.3}
\end{gather*}
$$

where $N_{\text {hot }}$ is the number of OMs with ADC and/or TDC rates greater than 30 $\mathrm{Hz}, N_{\text {dead }}$ is the number of OMs with ADC and/or TDC rates less than 0.5 Hz ,


Figure 6.1: The optical modules excluded from the 2000 analysis and their status.
and $N_{\text {unstable }}$ are the number of OMs with unstable ADC and/or TDC rates. The file cleaning removed about four percent of the events and reduced the detector live time to 197 days for the year.

### 6.2 OM Selection

An OM is considered bad if the ADC and/or TDC rate is too high, too low or zero, or if the number of edges from the TDC is too high. Figure 6.1 shows the OMs excluded in 2000.

In addition to the OMs above, other OMs were excluded on a time-dependent basis in an attempt to increase the effective area of the detector. These OMs demonstrated transient behavior, meaning at certain times of the year the OM operated normally and at others the $\mathrm{ADC} / \mathrm{TDC}$ rates demonstrated the behavior described above. In order to do this most efficiently, the year was divided into
three periods, with period 1 covering days $44-125$, period 2 covering days 126 244, and period 3 covering days 245-315.

### 6.3 Hit Cleaning

The data recorded by the AMANDA detector are not perfect. Each event has apparent hits due to various types of noise. The OMs themselves produce some of this noise; there is dark noise from the PMTs and noise produced by the decay of the radioactive potassium isotope ${ }^{40} \mathrm{~K}$ in the glass sphere which encases the PMT. The PMTs are also subject to pre-pulsing and after-pulsing. There is randomized cross-talk between OMs which can occur in the strings themselves or the surface electronics. In addition to all this, there is electronic noise in the DAQ.

Several criteria are used to reduce the number of hits due to noise. The calibrated amplitude is required to give a reasonable number of photoelectrons, 0.1 pe $<\mathrm{ADC}_{\text {calib }}<1000 \mathrm{pe}$. To eliminate random noise at the beginning and after-pulsing at the end, the event duration window is reduced to $-2000 \mathrm{~ns}<\mathrm{LE}<$ 4500 ns . Requirements of minimal amplitudes, $\mathrm{ADC}>20 \mathrm{mV}$, and time over thresholds, $124 \mathrm{~ns}<\mathrm{TOT}_{\text {elec }}<2000 \mathrm{~ns}$ for electrical and $5 \mathrm{~ns}<\mathrm{TOT}_{\text {elec }}<2000 \mathrm{~ns}$ for optically read out channels, reduces the electronic noise and electrical crosstalk. Finally, an isolation cut requiring a hit to be within 100 m and 500 ns of another hit eliminates hits due to random noise.

### 6.4 Filtering

The AMANDA data used in this thesis were recorded between February 13, 2000 and November 6, 2000. Over 1 billion events in 37,838 files took up 1.41 TB of disk space prior to filtering. Each file consists of approximately 10 minutes of data which were recorded by the DAQ electronics. The files were grouped into runs. Each run usually corresponds to one day of data taking. All files were then written to magnetic tape and transported north for final processing and storage.

The data used in this thesis were processed at the DESY Laboratory in Zeuthen Germany. Doing a complete 16 -iteration maximum likelihood reconstruction as described in section 5.2 is not practical with AMANDA's current resources. A 16-iteration maximum likelihood reconstruction takes approximately 1 second per event. Processing all 1.4 billion events would take approximately 4 months with the current AMANDA resources. As a consequence the AMANDA data is put through a series of filtering levels described below.

### 6.4.1 Level 1

In lieu of the full maximum likelihood reconstruction, a quick direct walk reconstruction as described in section 5.1 is performed on all events. This is the first fit placed on the data. Only events which pass the following cut

$$
\begin{equation*}
\theta_{D W}>70 \tag{6.4}
\end{equation*}
$$

are allowed to remain in the data set.
A full 16-iteration maximum likelihood reconstruction is then performed on
the remaining events. Another cut is placed on the data set,

$$
\begin{equation*}
\theta_{\text {fullfit }}>70 . \tag{6.5}
\end{equation*}
$$

The passing rate, after all selection criteria of level 1 are implemented, is $1 \%$.

### 6.4.2 Level 2

The data set is reduced further at the second level of data filtering. The first step of the level 2 filter is to place the following cut to the data

$$
\begin{equation*}
\theta_{\text {fullfit }}>80 \tag{6.6}
\end{equation*}
$$

where $f$ ull fit refers to the maximum likelihood reconstruction of level 1. Then six more reconstructions, including a multi-photon, a Bayesian, and several cascade reconstructions, are applied to the remaining data set. The passing rate of the level 2 filter is $0.4 \%$

### 6.5 Background Reduction

After the general filtering and cleaning procedures were applied, there were still non-neutrino backgrounds remaining in the sample. Further cleanings were performed to remove these backgrounds. These backgrounds can be attributed to electronic cross talk, coincident muon events from cosmic rays, and mis-reconstructed cosmic rays. Details of the procedures are described below.

### 6.5.1 Level 3 - Electronic Cross-Talk and Muons from Cosmic Rays

At level three two cleanings were performed. The first cleaning was used to remove electronic cross talk that results from capacitive coupling between ca-
bles. Secondly, a cut was developed to further remove muons in the data sample resulting from mis-reconstructed cosmic rays at the horizon.

Electronic cross-talk is known to occur between OMs located on the same strings in the twisted quad cables used in strings 5-10 of the AMANDA detector. This cross-talk cannot always be removed using basic cleaning algorithms. For this reason, a special hit cleaning was developed.

The first improvement to be made was to increase the TOT cut for hybrid OMs. Sixteen OMs have hybrid bases that were used for experimenting with optical transmission of signal to the surface. For normal data taking purposes, these channels are read out using the electrical output rather than the optical output. The electrical signal output for these OMs is much wider than that of normal OMs. Therefore, the minimum TOT requirement was increased from 120 ns to 200 ns for hybrid OMs. Thus, for standard and hybrid OMs, the minimum TOT required corresponds to $\sim 0.3$ pe.

Cross-talk maps of the detector were made for the 2000 data using timing calibration data. Using these maps, the unphysical regions of the ADC versus TOT plots were cut out with the program xt-filt. Figure 6.2 demonstrates visually how this was done. The boundary between the physical and unphysical region in the ADC versus TOT space has been fit by an exponential function. A shift of 20 mV in ADC and 20 ns in TOT is added to the ADC versus TOT distribution boundary to account for any fluctuations. More details about cross-talk in AMANDA can be found in $[48,49]$.


Figure 6.2: A demonstration of cross talk. The data points that cluster to the bottom-left of the solid curve are from cross talk. Taken from [48].

After the cross-talk cleaning was applied, two reconstructions were performed on the data. The first was the standard 16 -iteration maximum likelihood reconstruction described in section 5.2 . The second was a 16 -iteration maximum likelihood reconstruction with a Bayesian weighted prior as described in section 5.2.2. Events that had a likelihood ratio $\mathcal{L}_{u / d}<25$ (meaning they were more likely to have been produced by cosmic ray muons) were removed from the data sample.

The data passing rate after this level was $1.0 \times 10^{-4} \%$. The events removed by this level were mostly mis-reconstructed muons from cosmic rays and those that were triggered by electrical crosstalk.

### 6.5.2 Level 4 - Coincident Muons

The raw trigger rate of cosmic rays is $\sim 100 \mathrm{~Hz}$. That means every once in awhile two muons will enter the detector within a time scale of $\sim 5 \mu \mathrm{sec}$, close enough that they are treated as one "event" even though they are from two independent air showers. An example of a coincident muon event can be seen in Fig. 6.3. A detailed calculation of the rate at which these coincident muon events trigger the detector was performed in [50]. That rate was determined to be 0.69 per second.

At trigger level, the contribution from coincident muon events is quite low. Unfortunately, the criteria applied to events consider only a single muon hypothesis. This leads to an enhancement of the contribution from coincident muons at higher levels of the analysis. Therefore, a cut is applied at level 4 to reduce the


Figure 6.3: Example of a coincident muon event in the AMANDA-II detector.
coincident muon background contribution. That cut is a two-dimensional cut on zenith angle and the number of direct hits:

$$
\begin{equation*}
z e n i t h(u)-z e n i t h(d)<18.0 \times[n \operatorname{dirc}(u)-n \operatorname{dirc}(d)] \tag{6.7}
\end{equation*}
$$

where $u$ represents the standard 16 -iteration maximum likelihood reconstruction and $d$ represents the Bayesian reconstruction. This cut is demonstrated in Fig. 8.1.

### 6.6 Simulations

Generation of events, both neutrino and cosmic ray, occurs in three steps. First muon and neutrino events are generated. Then they are propagated through the ice to the detector. Finally, the detector response is simulated.

### 6.6.1 Muon Generation

Atmospheric muons are simulated using the generator CORSIKA [51]. The cosmic ray spectrum was assumed to be isotropic with a spectral index of $\gamma=2.73$ and energies between $8 \times 10^{2}$ to $1 \times 10^{9} \mathrm{GeV}$ nucleon ${ }^{-1}$. The interaction model used was QGSJET.

Simulating air showers requires an enormous amount of computer resources. The flux of cosmic ray primaries is isotropic and muons with energies above 600 GeV are deflected less than 1 degree. For these reasons, an event generated with CORSIKA is used multiple times by randomizing the azimuth angle and horizontal coordinates with respect to the detector. An oversampling factor of 100 was


Figure 6.4: Events to the left of the line are primarily due to mis-reconstructed cosmic ray muons and coincident muons.
used for this work. Physics fluctuations due to this oversampling rate are small compared to fluctuations due to the geometry and photon propagation.

Muons from neutrino events with energies between 10 GeV and 10 PeV are generated using NUSIM [52]. Not only does NUSIM generate neutrinos, it also propagates the neutrinos through the earth and simulates their interactions with nucleons. If a neutrino-nucleon interaction takes place in the earth, NUSIM will also propagate the muon through the rock to the rock-ice boundary using the MUDEDX code, which is based on tables calculated by Lohmann in [53].

### 6.6.2 Photon Propagation

Photon propagation in AMANDA is done using the program PTD [43]. The results of this program, mean amplitudes and arrival time distributions as a function of relative distance and orientation of the receiver, are stored in large multidimensional archives. These archives are known as the photon tables.

### 6.6.3 Muon Propagation in Ice

Muons from both neutrinos and cosmic rays are propagated through the ice and detector using MMC [54]. This program is capable of propagating muons that have energies from 105.7 MeV to $10^{11} \mathrm{GeV}$. Stochastic and continuous energy losses are calculated for particles with $\Delta \mathrm{E}>100 \mathrm{MeV}$. If $\Delta \mathrm{E}<100 \mathrm{MeV}$ only continuous energy loss due to ionization is taken into account. Ideally, all energy losses would be treated stochastically. However, as the energy of the particle increases, the number of separate energy loss calculations increases, which increases
the computation time [55]. The calculation of the muon's energy loss as it travels through ice is valid to within $1 \%$.

### 6.6.4 Detector Response

The detector response to muons beginning with the PMTs and ending with the DAQ system is simulated using AMASIM $[56,57]$. Rather than generating the timing and number of photon information for each OM itself, AMASIM gathers this information from tables generated by PTD.

Simulated parts of DAQ include the OM itself, the cable connecting the OMs to the surface electronics, the SWAMPs (Swedish amplifiers), the discriminators, the TDCs, the peak-sensing ADCs, and the trigger logic. A complete list of detector details and parameters taken into account by AMASIM is too long to list here. Even though much care has gone into producing the details of the detector simulation, more work needs to be done.

Some of the parameters needed for the simulation of the detector include positions of the optical modules and cable lengths. For simulating the OMs themselves, one also needs the noise rate, relative sensitivity, 1 photo-electron level, and the after-pulse probability of each OM.

## Chapter 7

## Atmospheric Neutrinos

Before embarking on the task of searching for high energy neutrinos from diffuse astronomical sources, it is imperative to have an understanding of the diffuse flux of neutrinos produced in Earth's atmosphere. These atmospheric neutrinos are not only a background to any search for high energy neutrinos, they also provide a known source which can be used to further understand and calibrate the detector.

Figure 7.1 shows the energy and zenith angle distributions of atmospheric neutrinos for 197 days, which corresponds to the detector live-time of AMANDAII for the year 2000. The energy spectrum of atmospheric neutrinos is steeper than that of their parent cosmic rays. The reason for this is that at high energies ( $\sim \mathrm{TeV}$ ), the pions that decay to produce neutrinos at lower energies start to interact rather than decay. The zenith angle distribution shows a peak in the atmospheric neutrinos near the horizon due to the longer flight times through the atmosphere that mesons have near the horizon.


Figure 7.1: The energy and zenith angle distributions of atmospheric neutrinos simulated for 197 days.

### 7.1 Level 5 - Event Quality

The basic tools used to determine the purity of any particular data set are simulations of cosmic ray muons, simulations of neutrinos, and the event viewer. Ideally, Monte Carlo simulations of down-going muons from cosmic rays and neutrinos alone would determine the purity. However, the simulations, although up-to-date with currently accepted theoretical models, are not accurate enough to be accepted at face value. One example of this is the atmospheric neutrino flux, which is input to the signal Monte Carlo. It has an uncertainty of $25 \%$ [58] at energies above 1 TeV .

The discrepancy between the Monte Carlo simulations and the data can be seen in Fig. 7.2. Plotted in this figure are the data and results from cosmic ray


Figure 7.2: The zenith angle distribution plotted for events passing level 4 criteria. muon, coincident muon, atmospheric neutrino, and $E^{-2}$ neutrino Monte Carlo simulations. By summing the simulation results in this figure, it is clear that the simulations alone can not account for all of the data events.

For these reasons, the idea of event quality was developed and applied at level 5 of this analysis. At first the quality cuts are applied loosely and deemed level 5.1 (level 5 processing, quality level 1 ). The cuts are then gradually tightened until level 5.8 (level 5 processing, quality level 8 ), where there are a handful of the best neutrino candidates left. This method is independent of the normalization to the neutrino flux discussed in 7.2 . Figures 7.3 and 7.4 show that as the quality parameters are tightened, the rate of change in the Monte Carlo and data begins to agree. This trend can also be seen in table 7.1.


Figure 7.3: The zenith angle distribution plotted for levels 5.1-5.4 As quality parameters are tightened, data and Monte Carlo simulations come into agreement. The solid line represents data, the dashed line represents atmospheric Monte Carlo simulations, and the dotted line represents the $E^{-2}$ Monte Carlo simulations.


Figure 7.4: The zenith angle distribution plotted for levels 5.5-5.8 As quality parameters are tightened, data and Monte Carlo simulations come into agreement. The solid line represents data, the dashed line represents atmospheric Monte Carlo simulations, and the dotted line represents the $E^{-2}$ Monte Carlo simulations.

Table 7.1: Passing rates of data and Monte Carlo simulations for various quality levels. The neutrino Monte Carlo has been normalized as described in 7.2.

| Level | Data | Atm. MC | $E^{-2} \mathrm{MC}$ | Atm $\mu$ MC | Coinc. $\mu \mathrm{MC}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 5.1 | 1388 | 819 | 121 | 69 | 68 |
| 5.2 | 1009 | 726 | 111 | 33 | 38 |
| 5.3 | 755 | 639 | 101 | 13 | 17 |
| 5.4 | 565 | 516 | 88 | 6.1 | 9.8 |
| 5.5 | 400 | 391 | 66 | 0 | 3.1 |
| 5.6 | 287 | 265 | 50 | 0 | 0.7 |
| 5.7 | 112 | 113 | 27 | 0 | 0 |
| 5.8 | 70 | 60 | 18 | 0 | 0 |

Before discussing the cuts developed at this level, it should be mentioned that cuts for levels 5.1-5.5 were based on 16-iteration maximum likelihood and Bayesian reconstructions. The level 5.5-5.8 cuts were based on more accurate 64-iteration maximum likelihood and Bayesian reconstructions.

There are a total of 6 quality cuts used in this analysis. Four of these cuts are one-dimensional. They are used to remove mis-reconstructed cosmic rays and coincident muons. All cuts used are based on the quality parameters described in section 5.3.

$$
\begin{gather*}
R_{L}^{u / d}=\log \frac{\mathcal{L}_{u p}}{\mathcal{L}_{\text {down }}}>35  \tag{7.1}\\
L_{\text {dir }}^{[-15: 25]}>155  \tag{7.2}\\
\left|S_{p h i t}\right|<0.275  \tag{7.3}\\
N_{d i r}^{[15: 75]}>10 \tag{7.4}
\end{gather*}
$$

Distributions comparing the data to Monte Carlo simulations of atmospheric
neutrinos and $E^{-2}$ of the one-dimensional cuts are shown in Figs. 7.5-7.8. In each of these figures, all cuts are applied except the one plotted. A vertical solid line represents the level of cut selected for the quality parameter in each plot. These plots have been constructed using the 100 percent data sample at level 5.5. In each plot, the number of Monte Carlo events have been normalized (see section 7.2) to the number of data events observed.

In addition to the one-dimensional cuts described above, a pair of twodimensional cuts are applied to the analysis. The first of these cuts was developed to remove unsimulated background events that fired more than 50 optical modules as they passed through the detector. This effect is shown in Fig. 7.9. Examining these events more closely revealed that they had positive values of the smoothness parameter as seen in Fig. 7.10. This meant that most of the light in the event was deposited in the second half of the track. The exact cause of these events is not fully understood. However, these events tend to be more spherical in nature (indicating shower-like behavior) and they also have shorter track lengths.

The following cut was developed to remove these events and is applied only to events that have more than 50 optical modules fired and positive smoothness.

$$
\begin{equation*}
L_{\text {dir }}^{[15: 75]}<4.3 *\left(\log \frac{\mathcal{L}_{\text {track }}}{\mathcal{L}_{\text {shower }}}\right)-65 \tag{7.5}
\end{equation*}
$$

The diagonal line in Figure 7.11 demonstrates the cut made to remove these events and figure 7.12 shows one of the events removed by this cut.

The final cuts were developed to ensure that events passing through only the very bottom or very top of the detector (where the optical modules are not


Figure 7.5: The likelihood of the events being up-going. Events to the right-hand side of the plot are most likely to be from up-going neutrinos. An excess of data events at lower values than the Monte Carlo simulations indicates that these events are likely to have been produced by down-going mis-reconstructed muons from cosmic rays rather than up-going neutrinos. Events to the left of the vertical solid line are removed.


Figure 7.6: The distance covered by the muon passing through the detector. Many mis-reconstructed tracks have lengths less than 155 meters. Events to the left of the solid vertical line are removed.


Figure 7.7: The distribution of the smoothness of the events in the detector. High quality tracks have smoothness values near 0 . Events between the two solid vertical lines are kept.


Figure 7.8: The number of hits in the detector with time residuals between -15 and 75 ns . A track with high quality would have many "direct" hits. Events to the left of the solid vertical line are removed.


Figure 7.9: This figure demonstrates the disagreement between data and Monte Carlo simulations for events that have more than 50 optical modules fired.


Figure 7.10: This figure shows the disagreement in the smoothness distribution for events that had more than 50 optical modules fired.


Figure 7.11: The direct length versus the negative log likelihood ratio of the the events being track-like to shower-like plotted for events with at least 50 optical modules fired and positive smoothness. Events above and to the left of the solid line are removed.



Figure 7.12: An event removed by the 2D cut on the length of the event versus the track-to-shower likelihood ratio applied to events with more than 50 optical modules fired which had a positive value of the smoothness parameter.
as evenly spaced as the middle of the detector) are from neutrinos and not misreconstructed comsic rays. These additional cuts were applied to tracks that had a zenith angle less than 120 degrees.

$$
\begin{align*}
& R_{L}^{t / s}=\log \frac{\mathcal{L}_{\text {track }}}{\mathcal{L}_{\text {shower }}}>-1.1 * \operatorname{cog} z-27.5  \tag{7.6}\\
& \operatorname{cog} z<150 . \tag{7.7}
\end{align*}
$$

These cuts are shown as solid lines in Fig 7.13.

### 7.2 Normalization

As mentioned in section 7.1, the flux of atmospheric neutrinos is known only to $25 \%$. In order to account for this fact the simulated neutrino flux is normalized to the observed flux of neutrinos. The ratio of the number of data events to the number of simulated events is plotted as a function of quality level in Fig 7.14. At low event qualities $(<4)$, the data are contaminated by background. At higher quality levels the ratio stablizes at 0.70 . This number agrees with the uncertainty in the atmospheric neutrino flux.

### 7.3 Other Atmospheric Neutrino Models

The model of atmospheric neutrinos used in this analysis was developed by Paolo Lipari [59] in 1992. His model uses analytic methods to compute the spectra of neutrinos and anti-neutrinos produced by cosmic rays in Earth's atmosphere.

In order to investigate the uncertainty introduced by the simulations of atmospheric neutrinos, two other atmospheric models were investigated for this


Figure 7.13: The track-to-shower likelihood ratio versus the center of gravity of the event. Events near the top and bottom of the detector, where optical modules are more sparsely placed, are required to demonstrate higher quality than events with center of gravities near the middle of the detector. Events below and to the left of the diagonal solid line and the events to the right of the vertical solid line are removed.


Figure 7.14: The ratio of number of events observed to the number predicted by Monte Carlo simulations of atmospheric neutrinos. The line fit at high event qualities shows the normalization factor used in this analysis.
analysis: one by Honda et al. [60] and the other by Agrawal et al. [61]. These fluxes are known as the "Honda" flux and the "Bartol" flux respectively. Both of these models use Monte Carlo simulations to determine their fluxes. The differences in the models primarily come from the assumed primary spectrum of cosmic rays and the hadronic interaction model in the atmosphere. In calculating the Honda flux, the authors use a higher primary spectrum normalization than that used by the authors of the Bartol flux.

The hadronic interaction model TARGET [62] used by the authors of the Bartol flux is a simple phenomenological representation of pion and kaon production in interactions of protons, pions, and kaons with light nuclei. The program uses parameterizations of accelerator data for hadron-nucleus collisions with emphasis on interaction energies around 20 GeV . The authors of the Honda flux used more sophisticated generators designed for studies at accelerators.

In their original work, the authors of the Honda flux calculated fluxes for neutrinos up to 31 TeV in energy and the authors of the Bartol flux calculated fluxes for neutrinos with energies up to 10 TeV , while the Lipari flux is calculated up to 316 TeV . Futher work by Gaisser [63] extended the Bartol flux up to 1 PeV making it easier to compare with the Lipari predictions and with the AMANDA data. Although the Honda flux predictions do not reach as high as those of Lipari and Bartol, one still can make comparisons of trends observed at lower energies. Figure 7.15 shows the absolute flux predictions, meaning the fluxes are not normalized. The difference in number of neutrinos predicted below 31 TeV
in energy between Lipari and Honda is $2.3 \%$ while the difference between Lipari and Gaisser was found to be $23.9 \%$.

To properly compare the different models for this analysis first one must convert to the energy parameter used for this analysis, the number of optical modules fired. Because of the uncertainty in the prediction of primary cosmic rays that produce atmospheric neutrinos, the observable difference in the models that we are interested in is not the total number of neutrinos predicted, but the spectrum these models predict. Thus, for comparison purposes the models are normalized to each other. Finally, a cut must be placed at a neutrino energy of 31 TeV , since the Honda flux only predicts energies up to that value.

Figure 7.16 shows the results of this analysis. There is no observable difference in the energy parameter of this analysis for the three models tested. The data is plotted against the three different models in Fig. 7.17. The apparent deficit in high values of the number of optical modules fired parameter can be explained by the fact that no energy cut was made for this plot since it is not possible to know the true energy of the neutrino in the data.


Figure 7.15: Neutrino energy for the three flux predictions used in this analysis. Below 31 TeV the Lipari and Honda fluxes agree to within $2.3 \%$ while the Bartol flux predicts 23.9 \% more neutrinos than the Lipari flux.


Figure 7.16: The number of optical modules fired for each event for energies less than 31 TeV plotted for the three models tested, Lipari, Bartol and Honda. The number of events for each model has been normalized to the Lipari model.


Figure 7.17: The number of optical models fired during each event plotted for data and the three models tested. The models have been normalized to the number of data events.

## Chapter 8

## Searching for a Diffuse Flux of High Energy Neutrinos

The search for neutrinos from diffuse astronomical sources was done using a blinded analysis technique. This technique required that an unblinded sample ( $50 \%$ of the year 2000 data in this case) be used for developing cuts and analysis techniques, while the remaining $50 \%$, the blinded sample, be untouched until after all cuts and techniques were fixed. The unblinded sample is used for the final analysis and the final result will then be free of any bias introduced by the scientist.

Before presenting the final results, one last review and check on the backgrounds to this analysis will be given as a firm understanding of the backgrounds is crucial for analyses that search for small signals. Then the final cut on energy will be optimized and the sensitivity of the experiment calculated. An effective area will be shown based on the final cut selection and the systematic uncertainties will be discussed. Finally, results will be shown for the assumed $E^{-2}$ neutrino
spectrum followed by a discussion of the results and limits on other high energy neutrino flux models.

### 8.1 Background Rejection

There are three main backgrounds to this analysis. Two of the backgrounds are muonic in origin - cosmic ray muons and coincident cosmic ray muons. The third background is the atmospheric neutrino background.

### 8.1.1 Cosmic Ray Muons

Single muons from cosmic rays are rather easy to remove from the $E^{-2}$ signal sample. This analysis used the techniques described in chapter 7 to remove single muons from cosmic rays. At the final cut level there is no contamination expected from single cosmic ray muons.

### 8.1.2 Coincident Muons

Coincident muons, which occur when two muons from independent air showers enter the detector at the same time and accidentally trigger the detector, are a little more tricky to remove. Using the cuts described in chapter 6 , at the level chosen for this analysis (level 5.5), 1.7 events from coincident muons are expected to remain in the sample according to Monte Carlo simulations of these events. However, in the energy range of particles considered in this analysis (see section 8.1.3), no coincident muon particles were observed.

The difficulty in concluding that this background would not affect the final
sample is that it is based on limited statistics. Coincident muon Monte Carlo simulations have been generated for 83.1 days of live-time using approximately 200,000 CPU hours of computation time.

A procedure to extrapolate to larger statistics was developed. This procedure is demonstrated in Fig 8.1. As the selection criteria are tightened, the number of events expected from coincident muons diminishes. In the region of interest for this analysis, an exponential function with a slope of -0.06 can be fit to level 3 and level 4 Monte Carlo simulations of coincident muon events. An assumption was made that this slope would remain constant as the cuts continued to be tightened. Extrapolating to level 5.1 still showed agreement with the simulations. Extrapolating further to level 5.5 gave an expectation of less than a hundredth of an event each year in the signal region. Thus, for this analysis it is assumed that the signal region of high energy neutrinos will not be contaminated by coincident muons.

### 8.1.3 Background Atmospheric Neutrinos

Atmospheric neutrinos are created during cosmic ray showers in the upper atmosphere. To the AMANDA detector, these neutrinos seem identical to the high energy $E^{-2}$ signal neutrinos in every way except their energy spectra.

This analysis uses an energy parameter to separate diffuse signal neutrinos from the diffuse atmospheric neutrino background. Figure 8.2 uses Monte Carlo simulations to show the energy spectrum of the muon as measured at the center of the detector for signal neutrinos and background atmospheric neutrinos. This


Figure 8.1: As selection criteria are tightened, the number of coincident muon events for a year diminishes. In the region where the number of optical modules fired in events is between 50 and 125, an exponential function can be fit to levels 3 and 4. Extrapolating this function to level 5.1 still shows agreement. Extrapolating to level 5.5 shows an expectation of less than a hundredth of an event each year in the signal region (nch $>80$ ).
plot shows that not only do the signal neutrinos have higher energy than the atmospheric neutrinos, the signal neutrinos have a different spectrum.

A very simple, but effective, energy parameter is to count the number of optical modules fired during an event. This parameter is known as nchannel. Figure 8.3 demonstrates the relationship between muon energy at the center of the detector and nchannel using Monte Carlo simulations of neutrino events. Figure 8.5 demonstrates that nchannel is an effective parameter for separating atmospheric neutrinos for $E^{-2}$ signal neutrino events.

### 8.2 Sensitivity

After deciding how to separate the atmospheric neutrino background from the $E^{-2}$ signal neutrinos, the detector sensitivity can be calculated. The method chosen for this analysis is that of the model rejection potential as described in section 5.4. Sensitivities and cuts based on the number of optical modules fired during an event were calculated. The results of the model rejection potential are outlined in table 8.1.

Table 8.1: Sensitivities and best number of optical modules fired cut for various detector live-times.

| Live-time [days] | Best \# OMs Fired Cut | Sensitivity $\left[\mathrm{cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}\right]$ |
| :---: | :---: | :---: |
| 98.6 | 80 | $3.8 \times 10^{-7}$ |
| 197 | 87 | $2.4 \times 10^{-7}$ |
| 400 | 89 | $1.5 \times 10^{-7}$ |
| 1000 | 95 | $0.9 \times 10^{-7}$ |



Figure 8.2: The muon energy at the center of the detector for atmospheric neutrinos (background) and $E^{-2}$ neutrinos (signal) before and after the nchannel cut.


Figure 8.3: The above plots demonstrate a relationship between the number of OMs fired during an event and the reconstructed muon energy at the center of the detector.


Figure 8.4: The number of optical modules fired during events. The dashed line represents the background atmospheric neutrino Monte Carlo and the dotted line represents the signal Monte Carlo.

### 8.3 Effective Area

Based on the selection criteria described in chapter 7 and the number of optical modules fired cut described above, it is possible to define an effective area for this analysis. The effective area is defined as

$$
\begin{equation*}
A_{e f f} \equiv\left\langle\frac{N_{\text {cuts }}}{N_{\text {gen }}} A_{\text {gen }}\right\rangle \tag{8.1}
\end{equation*}
$$

where $N_{\text {cuts }}$ is the number of events remaining in the sample after selection criteria are applied, $N_{\text {gen }}$ is the number of events generated in the sample, and $A_{\text {gen }}$ is the generation area of the events. An effective area given in this fashion is useful for comparison of theoretical predictions.

### 8.4 Systematic Uncertainties

The systematic uncertainties associated with the AMANDA detector are quite large when compared to other high energy detectors. This is due in part to the fact that neutrino telescopes such as AMANDA use natural media, i.e. ice, as a detector medium. The optical properties of the ice used by AMANDA are difficult to measure precisely. The process of deploying the optical modules requires a melting-refreezing process that may drastically affect the properties of the ice. Once deployed, the OMs are inaccessible. Thus, reasons for strange behavior in any OM after deployment can only be deduced from signals received by the surface electronics. The theoretical uncertainties associated with neutrino-nucleon interactions are higher for AMANDA compared to those of accelerator experiments, due to the higher energy particles the AMANDA detector investigates.


Figure 8.5: Effective area for the cuts used in this analysis.

The flux of atmospheric neutrinos is a convolution of the primary cosmic ray spectrum with the yield of the neutrinos produced by hadronic interactions of the cosmic rays in the atmosphere. Uncertainties in the primary cosmic ray spectrum and properties of relevant hadronic interactions affect the uncertainty of the atmospheric neutrino flux. This effect has been studied in [58] and is estimated to be approximately $30 \%$.

The rate of energy loss in ice is not precisely known. The propagation code MMC used in the AMANDA-II simulations uses the formulas for cross sections which are valid within $1 \%[54,55]$. For the energy range from 20 GeV to $10^{11} \mathrm{GeV}$, the coefficients a and b from formula 3.9 have an average deviation from the linear formula between $3 \%$ and $5 \%$ [36].

Approximations are made by PTD in the implementation of the measurements of the optical properties of the ice. This can be seen by comparing analysis results using the KGM ice model, where direct measurements of the optical properties were used by PTD, to the results of the MAM ice model, which is an evolution of the KGM model. However, the MAM model corrects the error introduced by the approximations made by PTD by adjusting the absorption coefficient of the ice. The absorption coefficient in the MAM ice model was derived from fits to the data.

The optical properties of the ice melted during deployment and then refreezed in the week following are difficult to measure. This quick refreezing process introduces many air bubbles in the ice nearest the optical modules. A camera
was deployed with one of the strings in the 1997-98 season. It indicated that there was very strong scattering near the optical modules. However, the issue could not be entirely settled as there was the possibility that the equipment simply failed. The lasers used for calibration purposes do not have a good line-of-sight through the bubbly ice to nearby modules. Thus, there are no direct measurements of the optical properties of hole ice.

Most of the uncertainties described above are absorbed by the normalization of the Monte Carlo simulations to the atmospheric neutrino flux. Thus, in the final analysis, only the atmospheric neutrino spectrum remains as the systematic uncertainty.

### 8.5 Results

As previously mentioned, this analysis was done using a blindness technique. As previously described, this technique required that $50 \%$ of the data be "blinded", meaning that this sample would not be touched until all cuts were refined. The remaining $50 \%$ would be used to develop cuts and the analysis technique. The final result would then be reported using only the blinded $50 \%$ sample.

The unblinded sample had a total of 222 neutrino candidates and a live-time of 98.4 days. Using the model rejection potential method described in 5.4, the number of optical modules fired cut was placed at 80 . The predicted number of high energy signal neutrino events was 11.8 and the predicted atmospheric background was 3.3 above the cut. After applying the cut to the data, 6 events
remained in the sample. This yielded a limit of $7.0 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$ without systematic uncertainties. Figure 8.6 shows the Monte Carlo distributions for atmospheric neutrinos and $\mathrm{E}^{-2}$ neutrinos along with the distribution in data for the number of optical modules fired parameter.

The blinded sample had a total of 178 neutrino candidates and a live-time of 98.6 days. The model rejection potential method yielded an optimal cut of the number of optical modules fired be greater than 80. Again, the predicted number of neutrino signal events was 11.8 and predicted number of background events was 3.3 above the cut. After applying the cut to the data, 4 events remained in the sample giving a limit of $4.5 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$ without systematic uncertainties. Figure 8.7 shows the Monte Carlo distributions for atmospheric neutrinos and $\mathrm{E}^{-2}$ neutrinos along with the distribution in data for the number of optical modules fired parameter.

Although it does not follow a strict blinding procedure, combining the samples together and running the analysis yields interesting results. The combined sample has 197 days of live-time and contains 400 neutrino candidates. The optimal number of optical modules fired cut is 87 according to the model rejection potential method. Above this cut, there are 21.0 predicted signal high energy neutrino events and 4.5 predicted atmospheric background neutrino events. There were 9 events observed above the cut. This yields (without systematic uncertainties) a two sided confidence band with boundaries of $0.9 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$ on the bottom side and $4.9 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$ on the high side. Figure


Figure 8.6: Number of channels fired for the unblinded data sample.


Figure 8.7: Number of channels fired for the blinded data sample.
8.8 shows the Monte Carlo distributions of atmospheric neutrinos and $\mathrm{E}^{-2}$ neutrinos along with the distribution in data for the number of optical modules fired parameter.

The Poisson error on the observed rate of atmospheric neutrinos is combined with the theoretical flux uncertainty to compute the correlations between background and efficiency for use in the probability distribution function used in the confidence interval construction. The theoretical flux uncertainty is taken about the best-fit flux $\hat{\Phi}$ and extended to $\pm 0.25 \times \Phi$. To incorporate these systematic uncertainties in the efficiencies into the limit calculations the prescription of Cousins and Highland [64], as implemented by Conrad et al. [65] with the unified Feldman-Cousins ordering and improved by a more appropriate choice of likelihood test [66] was used. Results from the three data samples are shown in 8.2.

Table 8.2: Results for the three different data samples.

| Sample | Predicted <br> Background | Predicted <br> Signal | No. Obs. <br> Events | Limit w/o Sys. <br> $\left[\mathrm{cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}\right]$ | Limit w/ Sys. <br> $\left[\mathrm{cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}\right]$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| unblinded | 3.25 | 11.80 | 6 | $7.0 \times 10^{-7}$ | $7.2 \times 10^{-7}$ |
| blinded | 3.26 | 11.82 | 4 | $4.5 \times 10^{-7}$ | $4.8 \times 10^{-7}$ |
| combined | 4.47 | 21.04 | 9 | $0.5-5.1 \times 10^{-7}$ | $0.4-5.4 \times 10^{-7}$ |

### 8.6 Discussion of Results

The six remaining events in unblinded sample were scanned using the AMANDA event viewer. All six events appeared to be of high quality and consistent with a high energy muon track. Six events is an upward fluctuation from the predicted


Figure 8.8: Number of channels fired for the combined data sample.
3.25 background events that gives an upward fluctuation in the final limit.

Scanning the four events that remained in the blinded analysis, which is the final result of this thesis, reveals one event that appears to be due to a coincident muon event, while the remaining three appear to be of good quality and consistent with a high energy muon track. This leads to the conclusion that either the extrapolation chosen in 8.1.2 is not valid, or we just happened to have an upward fluctuation of the background from nearly zero to one. To further test these hypotheses, more coincident muon background will need to be generated.

A positive outcome of these analyses is the fact that both the blinded and unblinded samples gave similar results, within statistical fluctuations. This suggests that the cuts chosen were good in the sense that they did not remove single, isolated background events, but whole classes of events.

Perhaps the most interesting of the results comes from the of the analysis that combined the blinded and unblinded data sets together. That analysis appears to give an excess of data events. At face value, it appears that a signal has been observed with a chance probablility of $3.7 \%$. However, one must be very cautious of interpreting this result. Firstly, scanning the remaining nine events revealed one event that appeared to be caused by a coincident muon event entering the detector. Taking that event out of the equation leaves eight events on a background of 4.5 , which leads to a chance probablity of $8.2 \%$. At the $95 \%$ confidence level, this results in an upper limit of $5.1 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$.

There are three possible explanations for this result. First, it could be
unsimulated background. Scanning the signal candidates revealed that one event appears to be from coincident muons. Futher studies could rule this out. Secondly, it could be a fluctuation in the data. Analysis of more data will reveal whether this is the case. The final possibility is that a signal has been observed.

In conclusion, although the results do not offer enough evidence to claim signal at this time, they do offer tantalizing hope that AMANDA-II may be close to a discovery.

### 8.7 Other Models

Four other models of high energy neutrinos were tested for this thesis. Two of these models SDSS [67, 68] and SSQC [23] are for core models of neutrino production in AGN. One model, SSBJ [23], makes a prediction for neutrino production in the jets of AGN. The final model, CharmD [69], is an optimistic model for production of charm neutrinos in the atmosphere. The sensitivities of these analyses are recorded in table 8.3 and the experimental results are recorded in table 8.4. Figure 8.9 compares Charm D and SDSS model predictions to the limits found in this analysis. Also shown in figure 8.9 is a comparsion of published AMANDA-B10 results to the results of this analysis.


Figure 8.9: Comparison of predictions of Charm and the SDSS model of AGN to the results of this analysis. Also plotted are the AMANDA-B10 results and the AMANDA-II results (this work) for an assumed flat $E^{-2}$ spectrum.

Table 8.3: Sensitivities for other models of high energy neutrinos. The optimal nchannel cut, predicted number of background events, and predicted number of signal events are shown. The average upper limit $\left(\bar{\mu}\left(n_{b}\right)\right)$ and average model rejection factor are shown with and without the inclusion of systematic uncertainties.

| Sample | nchannel <br> cut | Predicted <br> Background | Predicted <br> Signal | $\bar{\mu}\left(n_{b}\right)$ <br> w/o Sys. | $\bar{\mu}\left(n_{b}\right)$ <br> w/ Sys. | MRF <br> w/o Sys. | MRF <br> w/ Sys. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SDSS | 112 | 0.85 | 7.49 | 3.15 | 3.24 | 0.42 | 0.43 |
| SSQC | 101 | 1.30 | 17.0 | 3.49 | 3.57 | 0.21 | 0.21 |
| SSBJ | 80 | 3.25 | 9.87 | 4.51 | 4.69 | 0.46 | 0.47 |
| Charm | 50 | 16.2 | 4.85 | 8.19 | 8.85 | 1.69 | 1.82 |

Table 8.4: Experimental results for other models of high energy neutrinos. The number observed, the predicted number of background events, and the predicted number of signal events are shown. The experimental limits (event limit $\mu_{o} \equiv$ $\left.\mu\left(n_{o}, n_{b}\right)\right)$ are given with and without the inclusion of systematic uncertainties.

| Sample | Number <br> Observed | Predicted <br> Background | Predicted <br> Signal | $\mu\left(n_{o}\right)$ <br> w/o Sys. | $\mu\left(n_{o}\right)$ <br> w/ Sys. | MRF <br> w/o Sys. | MRF <br> w/ Sys. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SDSS | 2 | 0.85 | 7.49 | 5.06 | 5.28 | 0.68 | 0.70 |
| SSQC | 2 | 1.30 | 17.0 | 4.61 | 4.68 | 0.27 | 0.28 |
| SSBJ | 4 | 3.25 | 0.87 | 5.34 | 5.66 | 6.14 | 6.50 |
| Charm | 15 | 16.2 | 4.85 | 6.41 | 6.82 | 1.32 | 1.41 |

## Chapter 9

## Conclusions

A search for neutrinos from diffuse astronomical sources has been performed with the AMANDA-II neutrino detector using the data taken in year 2000. After reducing the background of $\sim 10^{9}$ down-going cosmic ray induced muons, 4 events remain in the sample. Monte Carlo simulations predict 3.25 atmospheric neutrino (background) events and 11.82 high energy $\mathrm{E}^{-2}$ neutrino (signal) events for 98.6 days of live-time of the AMANDA-II detector. This yields a limit, including systematic uncertainties, at the $90 \%$ confidence level of

$$
\begin{equation*}
\Phi_{90 \%} \leq 4.8 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV} \tag{9.1}
\end{equation*}
$$

This is a considerable improvement over the current published result based on the 1997 diffuse flux analysis which included 130 days of AMANDA-B10 detector live-time and produced a result of $\Phi_{90 \%} \leq 8.4 \times 10^{-7} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$.

This thesis has also investigated the uncertainty introduced by simulation of the atmospheric neutrino flux by studying three different atmospheric neutrino models (Lipari, Bartol and Honda). The result of this analysis shows virtually no
difference in the energy parameter, number of optical modules fired, used by this diffuse flux analysis.

With a further investigation of coincident muons in the detector, this analysis can be easily extended using the 2001 and 2002 AMANDA-II data.

Looking toward the future, the construction of the IceCube detector is scheduled to begin in 2004 and end in 2010. IceCube will be a considerable upgrade from the AMANDA-II detector as it will instrument $1 \mathrm{~km}^{3}$ of ice and contain $\sim 4000$ optical modules on 81 strings. After three years of operation, IceCube will be sensitive to a diffuse flux limit of $\Phi_{90 \%} \leq 4.2 \times 10^{-9} \mathrm{~cm}^{-2} \mathrm{~s}^{-1} \mathrm{sr}^{-1} \mathrm{GeV}$ [70]. Figure 9.1 compares the limit found in this work with the IceCube sensitivity after 3 years of operation.


Figure 9.1: Comparison of IceCube sensitivity after 3 years of operation to the limit set with this work.

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## Appendix A

## Reconstruction Chain

Table A.1: Outline of reconstruction chain.

| Level 1 |  |  |
| :---: | :---: | :---: |
| reco 1 | direct walk |  |
| reco 2 | maximum likelihood | 16 iterations |
| cut 1 | $\Theta_{\text {reco } 2}>70^{\circ}$ |  |
| Level 2 |  |  |
| cut 2 | $\Theta_{\text {reco } 2}>80^{\circ}$ |  |
| reco 3 | multi-photoelectron | 16 iterations |
| reco 4 | Bayesian likelihood | 16 iterations |
| reco 5 | line fit |  |
| reco 6 | dipole moment |  |
| reco 7 | tensor of inertia | amplitude weight $=1$ |
| reco 8 | cascade likelihood |  |
| Level 3 |  |  |
| xt-filter |  |  |
| reco 9 | maximum likelihood | 16 iteration |
| reco 10 | Bayesian likelihood | 16 iteration |
| Level 4 |  |  |
| cut 4 | $\begin{aligned} & \left(\Theta_{\text {reco } 9}-\Theta_{\text {reco } 10}\right)< \\ & 18\left(\text { ndirc }_{\text {reco } 9}-\text { ndirc } \text { reco } 10\right) \end{aligned}$ |  |
| Level 5 |  |  |
| cuts 5-11 | quality cuts level 5.5 |  |
| reco 11 | maximum likelihood | 64 iterations |
| reco 12 | Bayesian likelihood | 64 iterations |

## Appendix B

## Quality Levels

Table B.1: List of cuts defining each quality level. The two dimensional cuts in the two rows are defined by their slope and intercept.

| Quality <br> Level | $L_{\text {dir }}^{[-15: 25]}$ | $-\mathcal{L}_{u / d}$ | $\left\|S_{P_{h i t}}\right\|$ | $N_{\text {dir }}^{[-15: 75]}$ | $L_{\text {dir }}^{[-15: 75]}<m *-\mathcal{L}_{t / s}-b$ | $-\mathcal{L}_{t / s}>m * \operatorname{cogz}-b$ <br> and $\operatorname{cogz}<150(\mathrm{~m}, \mathrm{~b})$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 100.0 | 30 | 0.400 | 5 | $(4.3,-25)$ | $(-0.22,-5.5)$ |
| 2 | 110.0 | 31 | 0.370 | 6 | $(4.3,-35)$ | $(-0.44,-11.0)$ |
| 3 | 120.0 | 32 | 0.350 | 7 | $(4.3,-45)$ | $(-0.67,-16.75)$ |
| 4 | 130.0 | 34 | 0.330 | 8 | $(4.3,-55)$ | $(-0.89,-22.5)$ |
| 5 | 155.0 | 35 | 0.275 | 10 | $(4.3,-65)$ | $(-1.1,-27.5)$ |
| 6 | 170.0 | 37 | 0.250 | 12 | $(4.3,-70)$ | $(-1.32,-33.0)$ |
| 7 | 200.0 | 40 | 0.200 | 15 | $(4.3,-75)$ | $(-1.54,-38.5)$ |
| 8 | 210.0 | 42 | 0.180 | 17 | $(4.3,-85)$ | $(-1.77,-44.25)$ |

## Appendix C

## Atmospheric Neutrino Event Candidates

Table C.1: List of atmospheric neutrino events.

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2142814 | 160 | 123.301 | 320.828 | 15.2945 | 33.301 | 53.0652 | 57.9794 |
| 3185887 | 182 | 157.48 | 313.104 | 1.99119 | 67.481 | 129.394 | 5.46677 |
| 3593604 | 226 | 171.038 | 355.539 | 20.9636 | 81.038 | 114.693 | 22.1963 |
| 423496 | 269 | 121.552 | 118.105 | 1.29468 | 31.552 | 129.453 | -30.9872 |
| 481414 | 84 | 126.515 | 75.4717 | 23.666 | 36.516 | 107.249 | -24.1695 |
| 1332216 | 157 | 160.908 | 100.636 | 12.8708 | 70.907 | 122.836 | 46.2211 |
| 1760779 | 188 | 162.309 | 259.04 | 18.1623 | 72.308 | 102.969 | 28.905 |
| 1567697 | 300 | 128.435 | 170.983 | 4.7038 | 38.435 | 164.594 | -5.1114 |
| 2078330 | 150 | 148.356 | 349.003 | 13.8531 | 58.357 | 108.528 | 57.0691 |
| 938626 | 151 | 157.079 | 41.7212 | 5.49294 | 67.079 | 145.411 | 17.3849 |
| 866 | 154 | 168.069 | 226.651 | 7.74847 | 78.069 | 136.26 | 29.2533 |
| 2412706 | 159 | 138.845 | 176.048 | 0.654423 | 48.844 | 120.869 | -13.979 |
| 672095 | 164 | 143.794 | 212.819 | 11.9026 | 53.795 | 140.655 | 61.318 |
| 3914785 | 164 | 141.591 | 227.981 | 0.323957 | 51.592 | 117.879 | -10.9655 |
| 938476 | 177 | 129.698 | 334.05 | 14.2338 | 39.697 | 74.445 | 68.7569 |
| 3432923 | 179 | 152.855 | 165.484 | 12.7188 | 62.854 | 124.554 | 54.2481 |
| 1957663 | 187 | 171.513 | 258.842 | 18.6472 | 81.513 | 113.389 | 27.2718 |
| 4974272 | 201 | 132.437 | 52.7352 | 20.918 | 42.436 | 83.6236 | -1.70357 |
| 3282703 | 207 | 165.333 | 110.991 | 6.85558 | 75.332 | 139.32 | 26.1691 |
| 2135873 | 216 | 163.605 | 300.849 | 20.3077 | 73.605 | 106.718 | 20.141 |
| 955188 | 218 | 132.478 | 332.528 | 12.8398 | 42.479 | 123.662 | 74.6478 |
| 3336654 | 218 | 153.976 | 45.6379 | 18.925 | 63.975 | 94.2921 | 23.7548 |
| 3790473 | 218 | 156.349 | 197.532 | 10.8865 | 66.35 | 139.717 | 46.738 |

continued on next page

Table C.1: continued

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2089774 | 222 | 149.334 | 342.856 | 15.2368 | 59.334 | 95.6363 | 49.5412 |
| 3055268 | 222 | 130.835 | 157.585 | 7.97706 | 40.835 | 179.276 | 29.521 |
| 5392785 | 62 | 122.563 | 90.9242 | 14.7564 | 32.563 | 52.2915 | 64.7812 |
| 4953315 | 236 | 158.247 | 34.3877 | 21.1709 | 68.246 | 104.66 | 13.6336 |
| 1697 | 236 | 148.436 | 62.0133 | 22.1297 | 58.437 | 102.87 | 2.09094 |
| 4683242 | 241 | 155.039 | 33.0419 | 22.0432 | 65.039 | 106.304 | 7.77119 |
| 831360 | 259 | 128.149 | 74.2357 | 15.0015 | 38.15 | 63.3937 | 60.9445 |
| 2200836 | 264 | 136.095 | 31.8114 | 14.9069 | 46.096 | 79.1172 | 59.2005 |
| 28561 | 272 | 173.878 | 345.289 | 8.47128 | 83.879 | 129.347 | 29.4919 |
| 3002342 | 272 | 150.309 | 147.378 | 11.3483 | 60.309 | 141.586 | 53.4168 |
| 4839112 | 273 | 143.019 | 41.6718 | 3.20105 | 53.02 | 143.255 | -4.21166 |
| 2700849 | 285 | 134.222 | 5.96017 | 20.1339 | 44.223 | 80.0084 | 6.24693 |
| 3520175 | 67 | 127.734 | 50.6807 | 11.27 | 37.734 | 179.007 | 67.3704 |
| 215224 | 292 | 154.451 | 190.286 | 20.9048 | 64.452 | 100.618 | 12.4372 |
| 5331635 | 69 | 138.732 | 290.263 | 1.73171 | 48.731 | 131.777 | -13.2376 |
| 1896065 | 302 | 154.624 | 355.666 | 19.2475 | 64.623 | 95.5759 | 21.9064 |
| 3277996 | 307 | 148.84 | 76.7077 | 3.83664 | 58.84 | 144.316 | 3.60131 |
| 3948769 | 69 | 158.846 | 144.439 | 6.65749 | 68.845 | 146.188 | 24.1082 |
| 898909 | 72 | 144.404 | 62.0627 | 0.976479 | 54.405 | 123.984 | -8.45215 |
| 1229568 | 77 | 169.206 | 107.723 | 23.8249 | 79.207 | 119.94 | 16.6968 |
| 2851464 | 78 | 125.122 | 30.2293 | 11.0935 | 35.123 | 186.88 | 66.0701 |
| 2377102 | 88 | 174.298 | 312.258 | 15.2546 | 84.297 | 119. | 31.6893 |
| 4567259 | 89 | 146.837 | 292.785 | 0.916248 | 56.836 | 123.418 | -6.03241 |
| 715221 | 90 | 128.641 | 331.188 | 7.77793 | 38.64 | 181.109 | 26.7859 |
| 4717507 | 99 | 176.852 | 18.3145 | 14.1549 | 86.852 | 121.72 | 30.0911 |
| 597394 | 104 | 143.799 | 6.95995 | 23.6347 | 53.8 | 112.128 | -7.52582 |
| 2495921 | 106 | 154.377 | 304.518 | 10.6756 | 64.377 | 143.098 | 47.3006 |
| 2928444 | 106 | 163.767 | 13.0684 | 7.71865 | 73.767 | 141.188 | 29.5665 |
| 3374821 | 106 | 144.659 | 79.0094 | 5.00195 | 54.659 | 153.998 | 7.56312 |
| 471928 | 108 | 141.284 | 78.1579 | 11.3117 | 51.284 | 152.6 | 60.1678 |
| 488352 | 114 | 150.548 | 234.38 | 4.59569 | 60.549 | 147.315 | 8.79178 |
| 224809 | 121 | 136.436 | 261.797 | 2.43239 | 46.437 | 139.425 | -13.3861 |
| 5726476 | 53 | 156.085 | 15.6118 | 21.5908 | 66.084 | 104.81 | 10.3767 |
| 4384033 | 136 | 120.157 | 184.128 | 8.67769 | 30.157 | 193.819 | 35.5975 |
| 4819501 | 137 | 123.046 | 144.115 | 13.1171 | 33.047 | 94.2192 | 83.1897 |
| 5929236 | 137 | 142.154 | 180.975 | 15.1854 | 52.153 | 86.3581 | 53.8816 |
| 1329751 | 138 | 146.12 | 319.734 | 11.4465 | 56.121 | 144.783 | 57.2696 |
| 5281309 | 139 | 139.485 | 221.383 | 10.2231 | 49.485 | 165.624 | 52.439 |

continued on next page

Table C.1: continued

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 698547 | 139 | 129.877 | 134.497 | 21.3088 | 39.878 | 84.6945 | -6.69083 |
| 441286 | 140 | 135.683 | 91.4076 | 23.2315 | 45.683 | 105.646 | -13.8893 |
| 5303086 | 144 | 170.711 | 90.5342 | 18.2611 | 80.712 | 112.511 | 28.1859 |
| 1326220 | 147 | 156.324 | 253.651 | 16.5058 | 66.324 | 98.1264 | 38.6074 |
| 1355187 | 147 | 169.176 | 279.881 | 14.8774 | 79.175 | 116.178 | 36.312 |
| 2165291 | 148 | 168.978 | 188.852 | 0.624797 | 78.977 | 122.238 | 16.1241 |
| 2159840 | 150 | 155.558 | 334.368 | 15.179 | 65.557 | 103.103 | 45.8421 |
| 5046057 | 151 | 156.956 | 163.441 | 14.9526 | 66.957 | 105.91 | 45.795 |
| 1259101 | 152 | 148.04 | 239.72 | 17.6913 | 58.039 | 86.4415 | 31.9002 |
| 4121944 | 154 | 144.777 | 43.8361 | 19.7658 | 54.777 | 87.5412 | 14.57 |
| 4724656 | 56 | 150.867 | 134.574 | 10.1481 | 60.866 | 150.438 | 46.6437 |
| 4382518 | 156 | 164.71 | 125.773 | 14.4205 | 74.709 | 114.947 | 40.9323 |
| 4132334 | 158 | 128.583 | 4.93843 | 7.56419 | 38.583 | 180.434 | 24.3551 |
| 1451412 | 158 | 161.949 | 152.949 | 9.931 | 71.949 | 139.031 | 39.2177 |
| 1654509 | 165 | 163.482 | 164.479 | 19.2804 | 73.481 | 104.89 | 24.1542 |
| 2116222 | 165 | 145.461 | 236.572 | 16.4147 | 55.46 | 84.7647 | 42.5894 |
| 3681545 | 165 | 126.586 | 65.6443 | 10.359 | 36.586 | 186.78 | 57.0264 |
| 3910453 | 170 | 158.705 | 48.9174 | 0.123911 | 68.705 | 118.935 | 6.17543 |
| 2842511 | 171 | 163.534 | 244.9 | 6.68018 | 73.534 | 141.166 | 25.188 |
| 4576434 | 177 | 144.577 | 258.661 | 10.7645 | 54.577 | 154.075 | 54.2833 |
| 5194469 | 178 | 130.772 | 281.183 | 12.4235 | 40.771 | 142.754 | 75.3397 |
| 2419051 | 179 | 151.518 | 44.3909 | 16.3034 | 61.517 | 92.9051 | 41.5974 |
| 3521648 | 179 | 127.045 | 271.042 | 6.07552 | 37.044 | 174.953 | 7.48809 |
| 2049092 | 180 | 176.657 | 97.4777 | 11.1914 | 86.658 | 124.564 | 30.1479 |
| 475650 | 182 | 169.497 | 12.0137 | 10.0743 | 79.497 | 131.422 | 34.7077 |
| 1796076 | 183 | 121.582 | 225.448 | 2.00246 | 31.581 | 139.658 | -29.0493 |
| 4895669 | 185 | 129.333 | 13.9474 | 6.22779 | 39.332 | 173.747 | 10.141 |
| 1021126 | 188 | 156.129 | 58.1021 | 5.53369 | 66.128 | 146.405 | 17.1366 |
| 1580120 | 188 | 120.343 | 203.431 | 21.376 | 30.343 | 78.2904 | -13.8983 |
| 5955415 | 188 | 165.616 | 20.5008 | 21.5408 | 75.616 | 111.473 | 17.3874 |
| 573627 | 190 | 143.264 | 227.942 | 18.2724 | 53.265 | 81.5809 | 26.5271 |
| 5276912 | 200 | 142.607 | 287.681 | 6.88337 | 52.608 | 163.664 | 21.4671 |
| 2137011 | 202 | 173.463 | 328.557 | 18.956 | 83.464 | 115.61 | 26.7695 |
| 967389 | 203 | 146.052 | 234.65 | 19.9791 | 56.053 | 89.5763 | 13.5559 |
| 2658001 | 59 | 160.213 | 254.579 | 17.7397 | 70.214 | 100.699 | 31.0613 |
| 2491556 | 213 | 137.589 | 198.883 | 4.36925 | 47.59 | 155.381 | -1.56085 |
| 1283256 | 60 | 131.393 | 121.708 | 21.6951 | 41.392 | 88.9558 | -8.63567 |
| 3368601 | 60 | 132.827 | 260.446 | 20.0593 | 42.826 | 78.3839 | 6.19648 |
|  |  |  |  |  | 27 | 2 |  |

continued on next page

Table C.1: continued

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 332303 | 224 | 146.28 | 212.38 | 16.0317 | 56.281 | 87.1848 | 45.4234 |
| 4844368 | 226 | 144.917 | 77.1417 | 21.0874 | 54.916 | 94.1441 | 5.22988 |
| 332712 | 234 | 142.157 | 16.8533 | 6.7287 | 52.158 | 163.656 | 19.9813 |
| 3373864 | 234 | 164.451 | 188.451 | 8.8699 | 74.451 | 139.162 | 34.0048 |
| 3533809 | 239 | 122.233 | 1.66995 | 18.687 | 32.232 | 61.3614 | 16.0666 |
| 1331839 | 62 | 150.488 | 13.1948 | 5.32518 | 60.488 | 150.675 | 13.041 |
| 2762494 | 242 | 130.105 | 176.537 | 3.63934 | 40.104 | 154.347 | -12.3735 |
| 1501705 | 245 | 142.478 | 192.181 | 21.1552 | 52.479 | 92.7413 | 3.14568 |
| 1608536 | 249 | 122.409 | 152.723 | 0.621733 | 32.408 | 119.474 | -30.3688 |
| 2843674 | 249 | 136.579 | 162.221 | 5.88369 | 46.579 | 165.449 | 10.1921 |
| 389600 | 250 | 153.437 | 279.557 | 10.4432 | 63.438 | 145.631 | 46.799 |
| 3014760 | 250 | 139.583 | 30.6523 | 15.5662 | 49.584 | 79.9625 | 51.7251 |
| 3349658 | 63 | 138.652 | 98.9554 | 7.29776 | 48.651 | 168.945 | 24.2021 |
| 4106905 | 254 | 131.003 | 23.7858 | 21.395 | 41.003 | 86.1963 | -6.60053 |
| 1505225 | 255 | 153.091 | 155.948 | 0.227849 | 63.092 | 118.674 | 0.532882 |
| 1545291 | 256 | 130.297 | 204.843 | 21.2403 | 40.296 | 84.4509 | -5.83414 |
| 3300293 | 259 | 124.642 | 135.963 | 22.4683 | 34.641 | 92.1952 | -19.5373 |
| 486914 | 262 | 155.036 | 183.321 | 20.7263 | 65.037 | 100.386 | 13.7004 |
| 2922333 | 262 | 165.608 | 262.665 | 2.83529 | 75.608 | 130.231 | 14.4459 |
| 730347 | 263 | 142.868 | 128.872 | 1.61213 | 52.869 | 129.831 | -9.39499 |
| 2845681 | 263 | 131.118 | 320.542 | 22.7049 | 41.117 | 98.2515 | -15.4844 |
| 2957667 | 263 | 157.184 | 175.965 | 8.86973 | 67.184 | 147.552 | 36.4295 |
| 1172768 | 264 | 140.891 | 210.276 | 22.2424 | 50.892 | 99.342 | -4.65065 |
| 4140788 | 265 | 123.744 | 209.957 | 12.4412 | 33.745 | 160.515 | 81.4751 |
| 2032341 | 269 | 152.954 | 92.715 | 10.5472 | 62.953 | 145.501 | 47.6486 |
| 3415232 | 269 | 120.08 | 359.039 | 23.2524 | 30.08 | 99.2908 | -28.3338 |
| 1035338 | 65 | 154.838 | 310.995 | 8.51513 | 64.839 | 150.98 | 34.8786 |
| 2880198 | 276 | 146.659 | 66.9023 | 16.5711 | 56.66 | 85.9205 | 41.0362 |
| 3290529 | 276 | 146.046 | 160.172 | 12.2568 | 56.045 | 133.118 | 60.3651 |
| 2469576 | 277 | 149.12 | 217.346 | 4.60807 | 59.12 | 148.457 | 7.91186 |
| 3638945 | 277 | 163.501 | 115.012 | 16.8253 | 73.502 | 105.671 | 34.4309 |
| 2395528 | 278 | 165.341 | 113.902 | 10.9153 | 75.34 | 132.137 | 39.6347 |
| 2828443 | 279 | 135.854 | 153.399 | 10.3956 | 45.854 | 170.334 | 55.3592 |
| 745094 | 280 | 156.428 | 118.967 | 3.40547 | 66.429 | 137.399 | 7.95208 |
| 3618665 | 280 | 166.802 | 4.0705 | 0.410794 | 76.802 | 121.359 | 14.0121 |
| 2783371 | 66 | 132.613 | 272.037 | 17.8482 | 42.612 | 68.8669 | 28.6687 |
| 122072 | 282 | 170.758 | 18.4628 | 7.336 | 80.758 | 133.319 | 27.9001 |
| 1535236 | 285 | 133.78 | 34.7887 | 12.8876 | 43.781 | 121.788 | 73.3432 |

Table C.1: continued

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3407046 | 285 | 150.139 | 255.815 | 6.69194 | 60.139 | 155.404 | 22.1027 |
| 3686412 | 285 | 146.604 | 238.912 | 9.09088 | 56.604 | 160.14 | 40.6245 |
| 5212833 | 288 | 158.925 | 188.753 | 19.0549 | 68.925 | 99.7584 | 24.1381 |
| 1630711 | 294 | 122.09 | 35.9698 | 13.6043 | 32.09 | 62.6181 | 79.0758 |
| 2756856 | 295 | 163.899 | 233.49 | 5.4356 | 73.9 | 138.929 | 20.3861 |
| 1546608 | 296 | 122.909 | 77.7734 | 10.5021 | 32.908 | 193.507 | 59.0175 |
| 1320443 | 297 | 164.498 | 203.14 | 1.21961 | 74.499 | 124.413 | 11.6898 |
| 5032179 | 300 | 127.737 | 189.698 | 18.8912 | 37.738 | 67.649 | 15.8337 |
| 2401616 | 301 | 136.381 | 277.629 | 1.31719 | 46.38 | 127.882 | -16.2263 |
| 1553304 | 305 | 137.521 | 188.737 | 13.261 | 47.521 | 111.434 | 69.0629 |
| 2783736 | 71 | 159.939 | 225.74 | 20.8142 | 69.939 | 104.794 | 16.1807 |
| 5949917 | 75 | 128.221 | 44.9787 | 21.0613 | 38.22 | 81.501 | -5.70026 |
| 3569875 | 79 | 130.102 | 202.569 | 2.01478 | 40.103 | 137.07 | -20.8545 |
| 2308452 | 82 | 144.615 | 164.583 | 0.842262 | 54.616 | 122.8 | -8.25552 |
| 5509929 | 85 | 146.403 | 253.014 | 7.42531 | 56.403 | 160.794 | 26.9219 |
| 5850961 | 85 | 122.263 | 47.632 | 22.4788 | 32.263 | 90.9006 | -21.5874 |
| 2863674 | 91 | 180. | 333.446 | 16.0122 | 90. | 122.932 | 27.1283 |
| 3994675 | 50 | 147.359 | 211.138 | 2.45243 | 57.36 | 135.587 | -3.14128 |
| 4436099 | 50 | 138.402 | 74.9444 | 13.1403 | 48.402 | 115.234 | 68.4716 |
| 1782730 | 96 | 140.309 | 229.382 | 12.4651 | 50.309 | 132.337 | 66.3873 |
| 2839606 | 96 | 143.223 | 58.7723 | 3.82969 | 53.224 | 147.786 | -0.816065 |
| 5736570 | 97 | 149.732 | 151.515 | 8.88832 | 59.732 | 156.604 | 38.4087 |
| 2897298 | 102 | 146.631 | 197.718 | 19.4076 | 56.631 | 87.9974 | 18.0911 |
| 3871583 | 51 | 133.214 | 272.339 | 23.1064 | 43.214 | 103.366 | -15.631 |
| 1208393 | 111 | 137.175 | 20.748 | 21.6788 | 47.176 | 92.6722 | -4.18003 |
| 545025 | 115 | 143.808 | 113.705 | 12.83 | 53.808 | 123.47 | 63.3185 |
| 1747483 | 116 | 167.387 | 201.448 | 12.0469 | 77.387 | 126.344 | 39.4173 |
| 4294055 | 117 | 152.1 | 43.968 | 9.2771 | 62.099 | 152.669 | 40.505 |
| 4438509 | 120 | 170.291 | 325.107 | 15.1039 | 80.29 | 116.368 | 35.053 |
| 6014534 | 121 | 133.209 | 32.3442 | 16.5537 | 43.208 | 67.9635 | 42.8522 |
| 1349324 | 122 | 158.705 | 359.934 | 0.387539 | 68.705 | 120.365 | 5.97387 |
| 4929757 | 123 | 125.609 | 60.3763 | 10.7296 | 35.608 | 187.596 | 61.6041 |
| 1654462 | 125 | 143.525 | 336.005 | 8.77144 | 53.524 | 164.621 | 38.3773 |
| 2341138 | 52 | 132.901 | 254.129 | 16.7311 | 42.901 | 67.5518 | 40.9082 |
| 2310094 | 127 | 123.167 | 1.08217 | 10.2397 | 33.167 | 193.071 | 55.7164 |
| 1056477 | 129 | 122.112 | 20.9622 | 3.03159 | 32.112 | 152.692 | -23.1147 |
| 1864962 | 53 | 161.971 | 158.096 | 21.4393 | 71.972 | 108.448 | 15.1455 |
| 2309938 | 141 | 158.697 | 210.139 | 22.9407 | 68.698 | 112.766 | 8.12682 |
|  |  |  |  |  |  | 27 |  |

continued on next page

Table C.1: continued

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2718534 | 141 | 157.395 | 10.4207 | 13.8557 | 67.396 | 114.274 | 48.713 |
| 5391306 | 145 | 123.447 | 338.131 | 2.03713 | 33.447 | 139.492 | -27.1381 |
| 1567237 | 145 | 142.3 | 26.1094 | 8.35667 | 52.299 | 166.332 | 34.679 |
| 3123122 | 54 | 135.79 | 187.858 | 0.230789 | 45.79 | 116.109 | -16.5832 |
| 4953648 | 309 | 93.1463 | 178.728 | 8.16302 | 3.1463 | 219.227 | 18.8395 |
| 4833861 | 179 | 98.6532 | 7.95422 | 5.33362 | 8.6538 | 194.196 | -15.8506 |
| 826017 | 183 | 114.913 | 274.009 | 18.3395 | 24.914 | 52.4777 | 17.5277 |
| 787075 | 269 | 100.09 | 1.08217 | 10.8143 | 10.091 | 237.583 | 56.4851 |
| 1735409 | 292 | 117.646 | 28.7132 | 14.3782 | 27.646 | 39.679 | 69.7658 |
| 610793 | 152 | 146.961 | 9.33852 | 6.28661 | 56.962 | 157.478 | 18.0611 |
| 70296 | 275 | 155.234 | 300.36 | 11.8441 | 65.233 | 132.917 | 50.7004 |
| 372857 | 126 | 124.389 | 10.8272 | 1.51721 | 34.39 | 132.158 | -27.7714 |
| 1053797 | 150 | 122.096 | 185.512 | 20.3426 | 32.096 | 71.2429 | -2.49706 |
| 3819978 | 151 | 133.192 | 186.99 | 8.41382 | 43.193 | 177.434 | 34.6978 |
| 4211145 | 152 | 130.055 | 357.352 | 22.7799 | 40.056 | 98.4899 | -16.8271 |
| 2954433 | 152 | 135.142 | 24.7306 | 15.2372 | 45.142 | 74.8616 | 56.411 |
| 3926431 | 156 | 124.787 | 18.2815 | 19.6837 | 34.788 | 69.183 | 5.92664 |
| 3670860 | 158 | 176.157 | 357.468 | 6.03699 | 86.158 | 127.118 | 26.2476 |
| 4607462 | 164 | 129.998 | 35.6072 | 16.0199 | 39.997 | 63.6869 | 48.9583 |
| 1363912 | 166 | 139.995 | 216.736 | 14.4161 | 49.996 | 91.2074 | 60.9765 |
| 885675 | 173 | 166.465 | 206.238 | 22.3586 | 76.466 | 114.407 | 16.1432 |
| 399490 | 175 | 141.693 | 251.629 | 17.3146 | 51.694 | 78.7892 | 35.0723 |
| 1097197 | 176 | 167.594 | 197.697 | 23.9262 | 77.594 | 119.854 | 15.0574 |
| 408176 | 177 | 123.104 | 354.545 | 10.569 | 33.104 | 193.071 | 59.8534 |
| 5220970 | 58 | 153.045 | 84.629 | 14.2542 | 63.044 | 107.819 | 51.5545 |
| 913071 | 179 | 137.595 | 138.737 | 3.358 | 47.596 | 147.43 | -8.0117 |
| 2171437 | 179 | 149.639 | 271.833 | 0.0453062 | 59.638 | 116.803 | -2.65279 |
| 417433 | 182 | 171.043 | 24.434 | 8.98882 | 81.043 | 131.851 | 31.5872 |
| 2202190 | 182 | 125.29 | 330.485 | 20.4728 | 35.291 | 74.7933 | -1.98939 |
| 2002836 | 184 | 154.896 | 23.2145 | 16.5194 | 64.896 | 96.3761 | 39.0398 |
| 3059438 | 185 | 146.129 | 189.682 | 9.78907 | 56.128 | 158.423 | 46.3043 |
| 425222 | 188 | 128.405 | 79.4708 | 2.48962 | 38.405 | 143.23 | -20.5758 |
| 4894298 | 59 | 123.299 | 201.003 | 5.7198 | 33.298 | 176.009 | 1.83768 |
| 4075572 | 201 | 156.25 | 45.7807 | 17.3728 | 66.249 | 96.3534 | 33.5862 |
| 4138556 | 201 | 138.067 | 324.629 | 23.0636 | 48.066 | 104.988 | -11.0206 |
| 2854432 | 59 | 137.534 | 223.96 | 20.4876 | 47.534 | 84.8377 | 5.02673 |
| 64253 | 207 | 143.11 | 235.106 | 8.6283 | 53.11 | 165.264 | 37.1289 |
| 4111686 | 210 | 150.249 | 307.375 | 23.8308 | 60.248 | 115.357 | -1.71488 |

Table C.1: continued

| Event No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2087472 | 214 | 120.195 | 24.368 | 14.3604 | 30.195 | 47.0933 | 70.0133 |
| 3997456 | 60 | 161.111 | 272.602 | 21.4773 | 71.111 | 107.941 | 14.4146 |
| 4145067 | 216 | 153.852 | 155.865 | 15.2623 | 63.852 | 100.751 | 46.5788 |
| 856749 | 218 | 140.844 | 62.9911 | 6.35342 | 50.844 | 163.622 | 16.2402 |
| 5110864 | 222 | 149.488 | 56.1135 | 23.9809 | 59.488 | 116.294 | -2.70438 |
| 4243847 | 222 | 171.491 | 28.3012 | 21.9981 | 81.492 | 116.75 | 20.7624 |
| 2709871 | 224 | 176.473 | 250.805 | 0.302282 | 86.472 | 122.375 | 23.6364 |
| 3867415 | 224 | 165.116 | 148.894 | 12.355 | 75.115 | 125.524 | 41.8612 |
| 4222511 | 61 | 148.683 | 30.5095 | 14.4665 | 58.683 | 101.591 | 54.2615 |
| 1853106 | 226 | 133.986 | 17.3587 | 11.8046 | 43.985 | 155.858 | 68.8861 |
| 64573 | 227 | 136.021 | 108.244 | 21.9858 | 46.021 | 94.3862 | -7.08417 |
| 2337283 | 240 | 120.53 | 32.9705 | 11.0818 | 30.53 | 198.272 | 66.4772 |
| 6098983 | 63 | 124.971 | 41.919 | 20.9042 | 34.971 | 77.7819 | -6.37433 |
| 520134 | 242 | 143.055 | 326.37 | 7.23868 | 53.054 | 164.099 | 24.6923 |
| 1433197 | 242 | 150.6 | 14.3978 | 8.25326 | 60.601 | 156.329 | 33.6004 |
| 1475367 | 243 | 160.515 | 32.8441 | 7.30951 | 70.516 | 144.901 | 27.7059 |
| 2533885 | 243 | 121.846 | 207.008 | 0.640916 | 31.847 | 119.717 | -30.9437 |
| 3184282 | 244 | 133.994 | 70.1213 | 13.1146 | 43.994 | 113.479 | 72.8497 |
| 2901500 | 245 | 169.415 | 218.291 | 2.15779 | 79.414 | 126.612 | 17.104 |
| 361286 | 249 | 166.849 | 146.637 | 19.1691 | 76.848 | 108.404 | 25.3096 |
| 1565795 | 251 | 133.659 | 252.689 | 17.9315 | 43.66 | 70.2445 | 27.9906 |
| 2608500 | 252 | 131.398 | 37.3156 | 13.3543 | 41.398 | 101.612 | 74.4727 |
| 3739618 | 253 | 151.265 | 65.919 | 16.8298 | 61.264 | 91.1583 | 38.056 |
| 2669207 | 254 | 137.968 | 120.066 | 8.14955 | 47.968 | 171.384 | 32.4432 |
| 2683260 | 262 | 149.29 | 41.8146 | 16.4415 | 59.29 | 89.6505 | 41.3539 |
| 3208799 | 262 | 124.04 | 117.457 | 13.8539 | 34.041 | 64.8501 | 75.414 |
| 2084416 | 263 | 165.734 | 157.953 | 6.00622 | 75.734 | 138.086 | 23.17 |
| 2517339 | 263 | 137.743 | 228.179 | 3.32563 | 47.743 | 147.072 | -8.06635 |
| 3220315 | 264 | 161.142 | 259.754 | 4.38172 | 71.141 | 138.401 | 14.9419 |
| 44693 | 268 | 132.511 | 85.3651 | 1.62047 | 42.512 | 131.864 | -19.5642 |
| 2324445 | 269 | 129.858 | 129.8 | 9.43899 | 39.859 | 182.527 | 46.0237 |
| 2258153 | 271 | 168.887 | 163.375 | 6.71026 | 78.888 | 135.322 | 26.1571 |
| 3480654 | 271 | 134.321 | 22.9178 | 21.7268 | 44.321 | 91.1674 | -6.6618 |
| 3136000 | 273 | 164.347 | 125.861 | 13.6555 | 74.347 | 118.587 | 42.3748 |
| 2861464 | 276 | 174.331 | 50.2852 | 17.5915 | 84.33 | 116.81 | 28.8398 |
| 3671632 | 277 | 134.486 | 137.172 | 15.4986 | 44.486 | 72.2844 | 53.9604 |
| 4008483 | 279 | 139.526 | 86.3648 | 20.2842 | 49.527 | 85.3427 | 7.81967 |
| 2651168 | 280 | 162.562 | 323.052 | 22.6534 | 72.563 | 113.304 | 12.2111 |

continued on next page

Table C.1: continued

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1857451 | 66 | 147.826 | 33.3165 | 6.31646 | 57.826 | 156.728 | 18.6075 |
| 3427166 | 282 | 127.943 | 193.846 | 10.9902 | 37.944 | 181.114 | 64.164 |
| 1096311 | 283 | 121.318 | 119.473 | 5.19273 | 31.319 | 173.936 | -4.81381 |
| 1418387 | 284 | 159.005 | 205.53 | 0.995744 | 69.005 | 123.68 | 6.14532 |
| 1725932 | 284 | 126.853 | 194.835 | 3.13426 | 36.853 | 151.192 | -18.4115 |
| 3374037 | 285 | 140.405 | 258.216 | 6.38258 | 50.404 | 164.157 | 16.3225 |
| 3874632 | 285 | 147.389 | 62.8537 | 21.6829 | 57.39 | 99.4284 | 3.4848 |
| 1664954 | 289 | 134.027 | 69.7203 | 11.2595 | 44.026 | 165.415 | 64.3758 |
| 3466077 | 289 | 151.402 | 13.6342 | 22.9863 | 61.401 | 109.913 | 1.39969 |
| 1310392 | 290 | 160.573 | 159.837 | 3.77554 | 70.574 | 136.563 | 12.4912 |
| 4382458 | 290 | 138.902 | 129.102 | 19.6751 | 48.901 | 81.7555 | 12.6684 |
| 5410121 | 294 | 121.747 | 149.504 | 22.5761 | 31.746 | 91.7093 | -22.7004 |
| 2536284 | 296 | 126.207 | 325.892 | 22.3071 | 36.207 | 91.4141 | -17.1325 |
| 6429891 | 69 | 146.453 | 180.277 | 13.1512 | 56.453 | 117.982 | 60.5054 |
| 4110705 | 302 | 130.748 | 75.1751 | 23.563 | 40.747 | 107.411 | -19.7726 |
| 57191 | 70 | 158.269 | 41.6663 | 23.3167 | 68.268 | 114.514 | 6.92005 |
| 2509774 | 70 | 124.938 | 82.1295 | 5.7004 | 34.938 | 174.486 | 2.49464 |
| 6282589 | 71 | 154.629 | 18.7704 | 23.6704 | 64.629 | 115.395 | 2.80451 |
| 5920919 | 73 | 143.135 | 66.9792 | 18.7044 | 53.134 | 82.3995 | 22.7164 |
| 5698902 | 75 | 145.349 | 15.1174 | 22.1048 | 55.349 | 100.897 | -0.293644 |
| 1609785 | 75 | 149.191 | 123.065 | 0.126581 | 59.192 | 117.335 | -3.20246 |
| 2232184 | 75 | 159.834 | 321.926 | 13.2423 | 69.834 | 120.007 | 47.1629 |
| 4810010 | 78 | 149.455 | 215.072 | 6.01239 | 59.456 | 154.174 | 17.0664 |
| 2072549 | 78 | 159.076 | 106.921 | 3.0403 | 69.075 | 134.215 | 9.12375 |
| 5472179 | 81 | 170.453 | 109.519 | 16.3453 | 80.454 | 113.961 | 32.6759 |
| 1999164 | 82 | 120.813 | 2.15335 | 10.4443 | 30.813 | 197.517 | 58.2569 |
| 3524743 | 83 | 130.231 | 12.6894 | 15.889 | 40.231 | 64.2143 | 50.4391 |
| 5596961 | 84 | 143.014 | 284.446 | 6.00704 | 53.013 | 160.189 | 14.2421 |
| 4082255 | 85 | 128.548 | 317.197 | 21.4621 | 38.547 | 85.0109 | -8.89183 |
| 2412334 | 85 | 143.407 | 147.669 | 2.32781 | 53.406 | 135.974 | -7.21681 |
| 5035326 | 86 | 155.626 | 247.46 | 5.74957 | 65.626 | 147.514 | 18.0782 |
| 3797071 | 89 | 123.532 | 52.5594 | 14.1132 | 33.532 | 59.0376 | 72.5579 |
| 1295968 | 98 | 154.338 | 44.8634 | 23.1966 | 64.337 | 112.401 | 3.52183 |
| 5696224 | 99 | 146.038 | 47.3298 | 16.0931 | 56.038 | 86.6121 | 45.0236 |
| 4406198 | 99 | 156.654 | 66.2376 | 9.7716 | 66.655 | 145.409 | 41.4812 |
| 3147292 | 100 | 158.939 | 41.3477 | 7.24898 | 68.94 | 146.646 | 27.2751 |
| 177109 | 101 | 123.505 | 184.441 | 9.84895 | 33.505 | 192.254 | 50.8329 |
| 4439572 | 102 | 129.676 | 131.997 | 5.52849 | 39.676 | 169.381 | 3.30214 |

continued on next page

Table C.1: continued

| Event No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5333094 | 102 | 142.091 | 279.244 | 23.0533 | 52.092 | 106.565 | -7.30658 |
| 3664277 | 103 | 126.814 | 174.141 | 23.7658 | 36.815 | 108.604 | -24.228 |
| 1299152 | 108 | 152.243 | 187.336 | 7.15014 | 62.243 | 153.981 | 25.8019 |
| 3162260 | 109 | 123.859 | 301.343 | 6.83024 | 33.858 | 181.954 | 14.4071 |
| 4527543 | 114 | 157.568 | 14.7274 | 11.0817 | 67.568 | 137.314 | 46.4733 |
| 3273134 | 115 | 137.238 | 79.2676 | 1.79792 | 47.237 | 132.778 | -14.5529 |
| 4693634 | 52 | 131.124 | 12.3214 | 20.0266 | 41.125 | 76.7353 | 5.61608 |
| 5817674 | 118 | 139.43 | 131.618 | 9.6798 | 49.429 | 168.199 | 47.4097 |
| 2163722 | 119 | 138.996 | 125.817 | 19.0891 | 48.996 | 79.4179 | 17.981 |
| 5528885 | 120 | 127.795 | 194.466 | 4.24304 | 37.795 | 161.305 | -9.50765 |
| 2085362 | 121 | 159.648 | 312.461 | 6.31243 | 69.647 | 144.819 | 22.5513 |
| 2905292 | 121 | 143.555 | 122.203 | 22.2365 | 53.556 | 100.803 | -2.4207 |
| 4285190 | 123 | 125.971 | 226.02 | 21.1822 | 35.972 | 80.7908 | -8.27848 |
| 5637104 | 123 | 146.497 | 100.812 | 10.7725 | 56.496 | 151.467 | 53.1408 |
| 1947477 | 125 | 139.734 | 59.6402 | 4.35191 | 49.735 | 153.743 | -0.164507 |
| 5619504 | 126 | 129.597 | 32.6574 | 20.4216 | 39.598 | 77.9467 | 1.00716 |
| 1590528 | 128 | 158.527 | 91.5669 | 1.31642 | 68.526 | 125.461 | 5.78961 |
| 3465006 | 133 | 121.085 | 156.634 | 6.57829 | 31.086 | 183.189 | 10.3588 |
| 2846119 | 134 | 160.903 | 267.56 | 20.8551 | 70.904 | 105.731 | 16.5861 |
| 3385603 | 135 | 155.989 | 210.342 | 2.79084 | 65.989 | 134.369 | 5.72736 |
| 2719596 | 136 | 131.242 | 64.3973 | 9.91933 | 41.241 | 179.877 | 51.3916 |
| 4144367 | 137 | 154.042 | 52.8725 | 16.6696 | 64.042 | 94.9384 | 38.3964 |
| 5157441 | 138 | 125.1 | 140.605 | 14.9128 | 35.1 | 57.4674 | 62.5522 |
| 1530546 | 139 | 134.104 | 255.227 | 16.5842 | 44.105 | 69.1732 | 42.5018 |
| 4563241 | 143 | 166.371 | 318.581 | 0.2129 | 76.37 | 120.598 | 13.6738 |
| 2072713 | 145 | 123.969 | 39.2383 | 9.47048 | 33.97 | 191.038 | 46.1585 |
| 509647 | 156 | 147.296 | 108.069 | 23.065 | 57.295 | 108.775 | -2.59088 |
| 1218145 | 162 | 142.613 | 155.97 | 17.9482 | 52.612 | 80.3379 | 29.3212 |
| 2533762 | 162 | 123.01 | 12.9421 | 9.09552 | 33.011 | 191.56 | 41.3864 |
| 129583 | 202 | 132.494 | 82.7558 | 2.27611 | 42.495 | 139.244 | -17.6644 |
| 2248138 | 207 | 136.647 | 278.096 | 15.2755 | 46.647 | 77.1187 | 55.5009 |
| 3878658 | 154 | 107.64 | 250.316 | 4.93773 | 17.64 | 183.096 | -15.684 |
| 1614328 | 55 | 98.233 | 246.564 | 14.7083 | 8.2336 | 2.40421 | 57.6405 |
| 4234847 | 260 | 94.2779 | 235.798 | 10.8853 | 4.278 | 246.694 | 53.6928 |
| 3187840 | 275 | 107.69 | 211.182 | 8.21673 | 17.689 | 205.338 | 25.721 |
| 1468281 | 87 | 106.451 | 1.69741 | 8.16384 | 16.451 | 206.281 | 24.5465 |
| 1695899 | 130 | 105.704 | 138.737 | 21.9214 | 15.705 | 72.6765 | -29.503 |
| 2410775 | 175 | 104.149 | 255.26 | 1.77024 | 14.15 | 142.462 | -46.6341 |

Table C.1: continued

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4275575 | 177 | 111.038 | 242.994 | 10.5184 | 21.037 | 216.003 | 57.5039 |
| 1157143 | 58 | 110.335 | 359.308 | 5.40023 | 20.336 | 184.639 | -8.75464 |
| 1958212 | 191 | 115.18 | 244.796 | 23.5113 | 25.18 | 100.748 | -34.1891 |
| 2785061 | 191 | 114.482 | 9.49783 | 18.8892 | 24.483 | 55.1812 | 10.4982 |
| 3844587 | 59 | 102.902 | 237.665 | 23.1287 | 12.902 | 87.4741 | -42.7173 |
| 3494149 | 218 | 117.069 | 67.8471 | 18.1695 | 27.069 | 53.7034 | 20.4522 |
| 89496 | 224 | 103.056 | 6.28428 | 4.69685 | 13.057 | 184.833 | -21.1998 |
| 1573409 | 245 | 110.56 | 184.853 | 21.9905 | 20.56 | 77.3061 | -26.6974 |
| 151289 | 63 | 103.682 | 96.5878 | 19.5542 | 13.682 | 49.8647 | -2.81127 |
| 4345784 | 253 | 103.625 | 73.8732 | 19.1937 | 13.625 | 47.3358 | 1.7953 |
| 1025334 | 64 | 95.4781 | 46.7915 | 2.19093 | 5.4768 | 156.588 | -52.0878 |
| 1368619 | 267 | 111.406 | 57.2781 | 9.52643 | 21.405 | 208.782 | 44.382 |
| 2511909 | 65 | 108.915 | 6.08652 | 10.3121 | 18.915 | 217.877 | 54.0619 |
| 1339798 | 272 | 108.599 | 229.173 | 22.3178 | 18.598 | 79.7922 | -31.2274 |
| 466376 | 276 | 92.965 | 29.0428 | 7.85537 | 2.9645 | 217.177 | 14.6661 |
| 4061847 | 285 | 113.15 | 53.8064 | 23.1375 | 23.151 | 94.1161 | -33.8825 |
| 3341036 | 292 | 112.202 | 96.5054 | 16.9966 | 22.202 | 42.5524 | 33.919 |
| 722405 | 78 | 119.118 | 155.778 | 18.6944 | 29.119 | 58.4208 | 14.7763 |
| 5398463 | 80 | 116.902 | 18.0288 | 21.0216 | 26.901 | 72.4634 | -12.6923 |
| 5779172 | 83 | 108.961 | 253.134 | 8.69341 | 18.962 | 206.82 | 32.5042 |
| 2500629 | 83 | 107.072 | 208.59 | 22.7537 | 17.073 | 84.602 | -36.2357 |
| 6034289 | 48 | 106.926 | 24.5054 | 0.791221 | 16.926 | 121.568 | -45.9352 |
| 168983 | 85 | 116.767 | 27.241 | 1.69792 | 26.766 | 136.656 | -34.758 |
| 2906243 | 85 | 107.019 | 251.371 | 21.2837 | 17.02 | 66.9352 | -21.8076 |
| 2915911 | 85 | 113.801 | 355.43 | 14.3834 | 23.801 | 28.8846 | 69.0969 |
| 2969523 | 94 | 101.578 | 149.334 | 22.3898 | 11.578 | 75.1625 | -37.2059 |
| 1133276 | 110 | 116.193 | 149.493 | 12.507 | 26.193 | 223.009 | 85.2126 |
| 2613026 | 112 | 103.375 | 267.95 | 11.0051 | 13.375 | 235.298 | 60.6348 |
| 2070666 | 121 | 100.491 | 204.552 | 13.4486 | 10.492 | 331.284 | 71.3839 |
| 1619568 | 123 | 101.221 | 215.951 | 11.0698 | 11.22 | 239.991 | 60.2093 |
| 3071680 | 126 | 108.714 | 282.529 | 18.4233 | 18.714 | 47.0441 | 13.997 |
| 5329687 | 128 | 109.357 | 218.532 | 8.19678 | 19.356 | 203.501 | 26.0776 |
| 3279091 | 129 | 101.059 | 192.747 | 0.590046 | 11.06 | 116.588 | -51.6141 |
| 5696095 | 141 | 104.512 | 25.9007 | 0.248638 | 14.511 | 109.808 | -47.428 |
| 1974873 | 143 | 108.255 | 195.406 | 22.3983 | 18.256 | 80.5738 | -32.22 |

## Appendix D

## High Energy Neutrino Candidates

Table D.1: List of high energy neutrino events for the blind sample.

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3878658 | 154 | 107.64 | 250.316 | 4.93773 | 17.64 | 183.096 | -15.684 |
| 1614328 | 55 | 98.233 | 246.564 | 14.7083 | 8.2336 | 2.40421 | 57.6405 |
| 1157143 | 58 | 110.335 | 359.308 | 5.40023 | 20.336 | 184.639 | -8.75464 |
| 70296 | 275 | 155.234 | 300.36 | 11.8441 | 65.233 | 132.917 | 50.7004 |

Table D.2: List of high energy neutrino events for the unblind sample.

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4953648 | 309 | 93.1463 | 178.728 | 8.16302 | 3.1463 | 219.227 | 18.8395 |
| 1735409 | 292 | 117.646 | 28.7132 | 14.3782 | 27.646 | 39.679 | 69.7658 |
| 234639 | 266 | 100.749 | 258.897 | 14.8255 | 10.748 | 8.11754 | 57.7666 |
| 3593604 | 226 | 171.038 | 355.539 | 20.9636 | 81.038 | 114.693 | 22.1963 |
| 1760779 | 188 | 162.309 | 259.04 | 18.1623 | 72.308 | 102.969 | 28.905 |
| 1355187 | 147 | 169.176 | 279.881 | 14.8774 | 79.175 | 116.178 | 36.312 |

Table D.3: List of high energy neutrino events for the combined sample.

| Event <br> No. | Day | Zenith | Azimuth | Right <br> Asc. | Declin. | Gal. <br> Long. | Gal. <br> Lat. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4953648 | 309 | 93.1463 | 178.728 | 8.16302 | 3.1463 | 219.227 | 18.8395 |
| 1735409 | 292 | 117.646 | 28.7132 | 14.3782 | 27.646 | 39.679 | 69.7658 |
| 234639 | 266 | 100.749 | 258.897 | 14.8255 | 10.748 | 8.11754 | 57.7666 |
| 3593604 | 226 | 171.038 | 355.539 | 20.9636 | 81.038 | 114.693 | 22.1963 |
| 1760779 | 188 | 162.309 | 259.04 | 18.1623 | 72.308 | 102.969 | 28.905 |
| 3878658 | 154 | 107.64 | 250.316 | 4.93773 | 17.64 | 183.096 | -15.684 |
| 1614328 | 55 | 98.233 | 246.564 | 14.7083 | 8.2336 | 2.40421 | 57.6405 |
| 1157143 | 58 | 110.335 | 359.308 | 5.40023 | 20.336 | 184.639 | -8.75464 |
| 70296 | 275 | 155.234 | 300.36 | 11.8441 | 65.233 | 132.917 | 50.7004 |

